

Surface plasmon polaritons (SPP): an alternative to cavity QED

Strong coupling to excitons &
Intermediary for quantum entanglement

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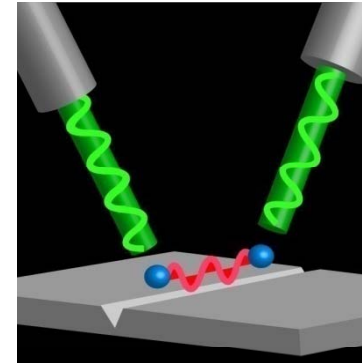
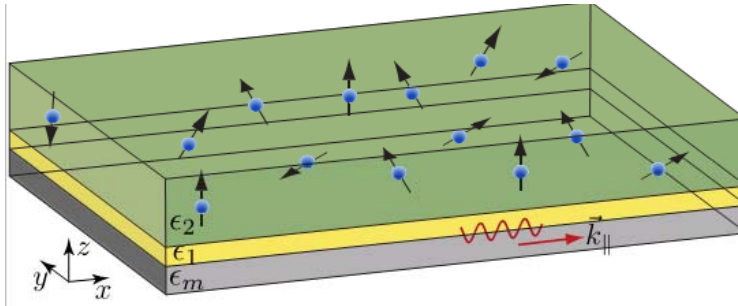
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CSIC*



SPP

Strong coupling to excitons &

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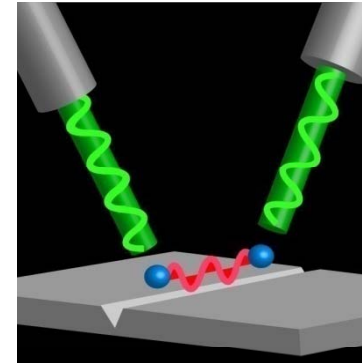
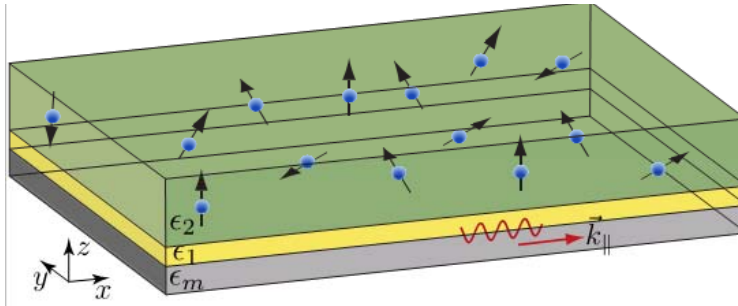
Outline

- Introduction to surface plasmon polaritons (SPP)
- Coupling of 1 quantum emitter (QE) to SPP
- Collective mode (excitons) strongly coupled to SPP
- Coupling & entanglement of 2 QE mediated by SPP
- Conclusion

SPP

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Intro: Surface plasmon polaritons

- Dielectric response of a metal is governed by free electron plasma:

$$\varepsilon(\omega) = 1 - \frac{\omega_p^2}{\omega(\omega + i\gamma)}$$

ω_p : plasma frequency
 γ : damping factor

Below its plasma frequency $\varepsilon(\omega)$ is negative...



wavevector : $k = \frac{\omega \sqrt{\varepsilon}}{c}$ → purely imaginary → photonic insulator

What is a surface plasmon polariton ?

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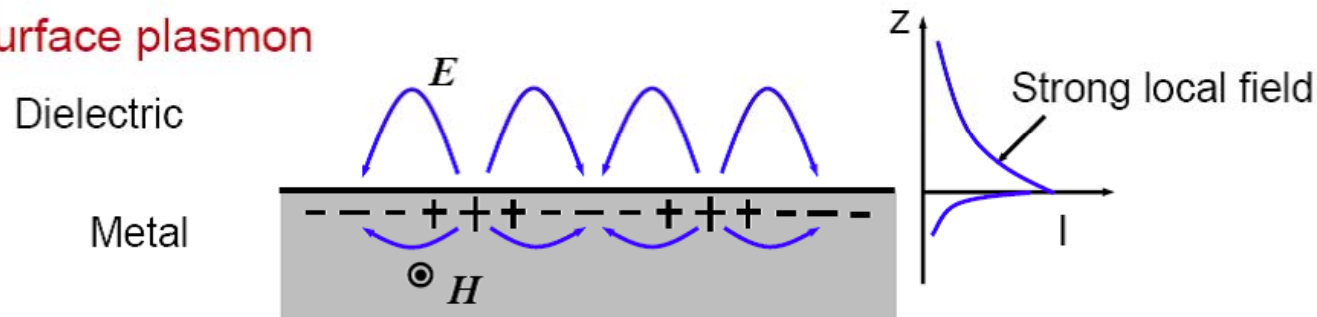
wavevector : $k = \frac{\omega \sqrt{\epsilon}}{c}$ → **purely imaginary** → **photonic insulator**

What is a surface plasmon polariton ?

Bulk plasmon

- Metals allow for EM wave propagation above the plasma frequency
- ↖ They become transparent!

Surface plasmon



Note: SP is a TM wave!

- Sometimes called a surface plasmon-polariton (strong coupling to EM field)

Intro: Surface plasmon polaritons

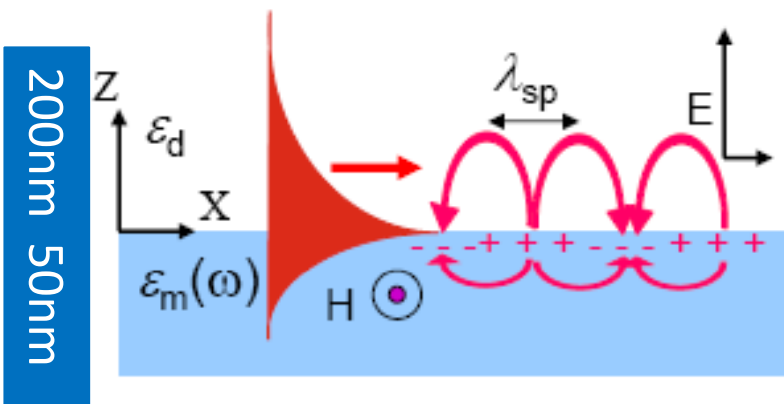
Electromagnetic radiation in dielectric \oplus Localized Plasmons in a metal surface



SURFACE PLASMON POLARITONS

1. SPPs are primarily transverse in dielectrics but longitudinal in metals!

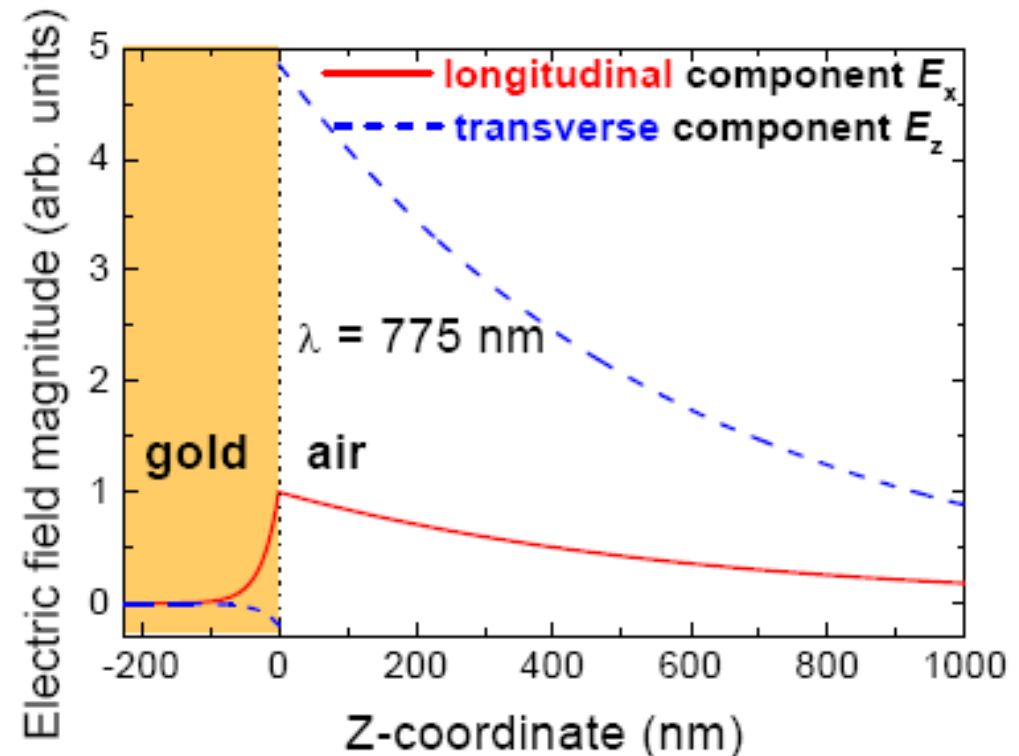
2. SPP properties are dictated by the boundary conditions for E_{\parallel} and E_{\perp} !



$$E_z^d = i \sqrt{-\epsilon_m / \epsilon_d} E_x^0$$

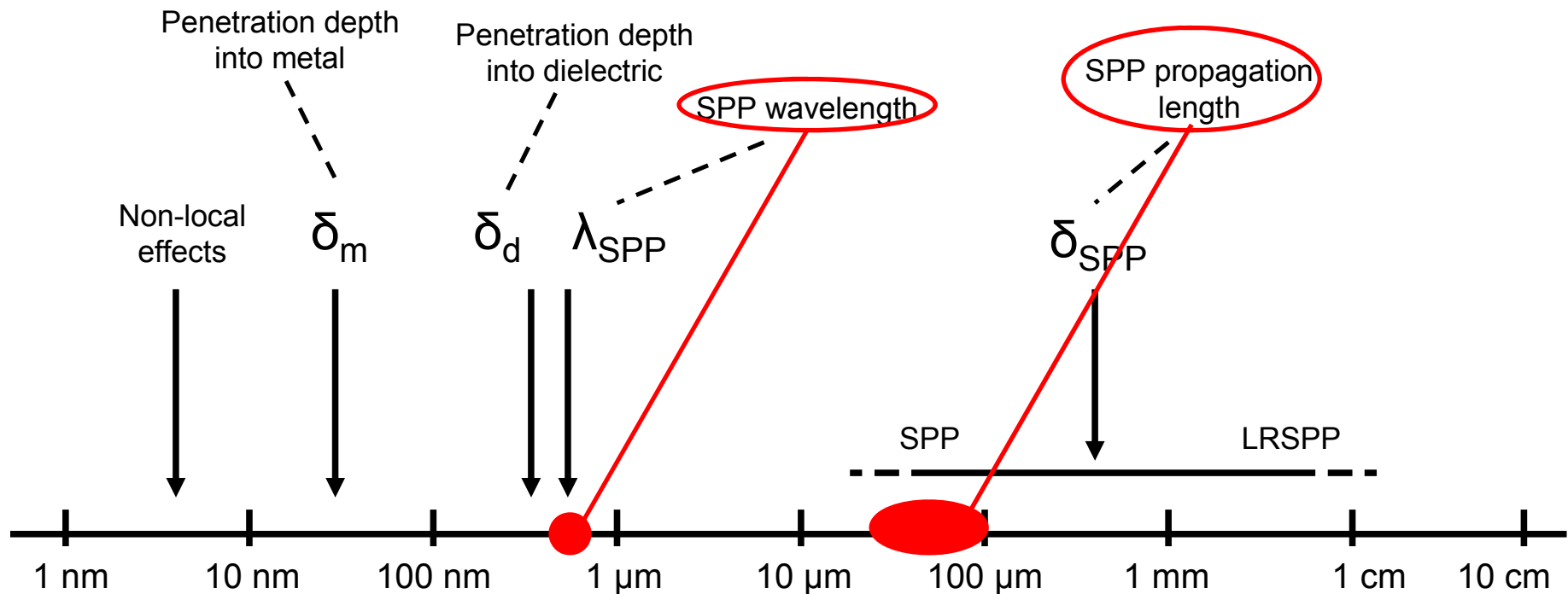
and

$$E_z^m = -i \sqrt{-\epsilon_d / \epsilon_m} E_x^0$$



Intro: Surface plasmon polaritons

SPP Length Scales span photonics and nano



Length scales span 7 orders of magnitude!

Intro: Surface plasmon polaritons

Plasmonics: Merging Photonics and Electronics at Nanoscale Dimensions

Ekmel Ozbay, Science, vol.311, pp.189-193 (13 Jan. 2006).

Roadmap for plasmonics

Some of the challenges that face plasmonics research in the coming years are

- (i) demonstrate optical frequency **subwavelength metallic wired circuits** with a propagation loss that is comparable to conventional optical waveguides;
- (ii) develop highly efficient **plasmonic organic and inorganic LEDs** with tunable radiation properties;
- (iii) achieve **active control of plasmonic signals** by implementing electro-optic, all-optical, and piezoelectric modulation and gain mechanisms to plasmonic structures;
- (iv) demonstrate **2D plasmonic optical components**, including lenses and grating couplers, that can couple single mode fiber directly to plasmonic circuits;
- (v) develop **deep subwavelength plasmonic nanolithography** over large surfaces;
- (vi) develop highly sensitive **plasmonic sensors** that can couple to conventional waveguides;
- (vii) demonstrate **quantum information processing by mesoscopic plasmonics**.

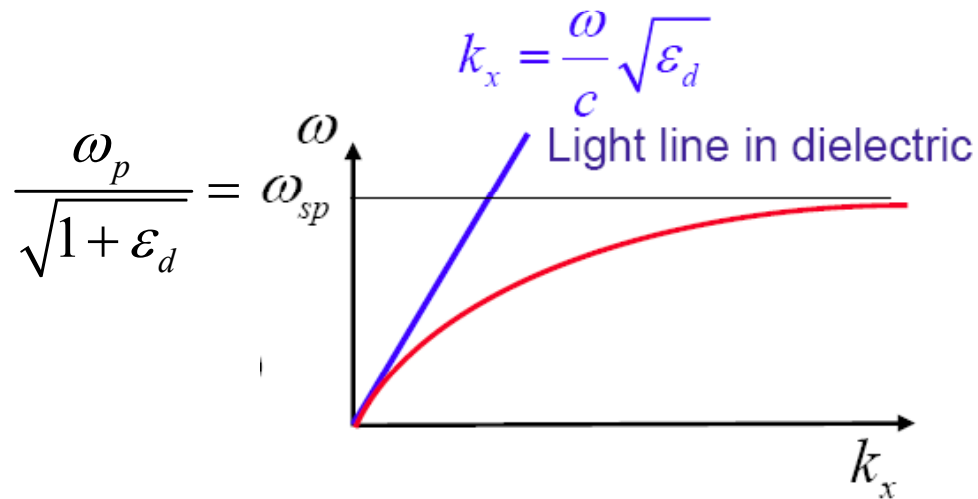
Intro: Surface plasmon polaritons

- **Interesting features of SPPs for photonic circuits:**
 - Propagation length: 50-100 μm (Ag or Au) \Leftrightarrow lifetime ≤ 1 ps
 - Two-dimensional character of EM-fields
 - Optical and electrical signals carried without interference

Intro: Surface plasmon polaritons

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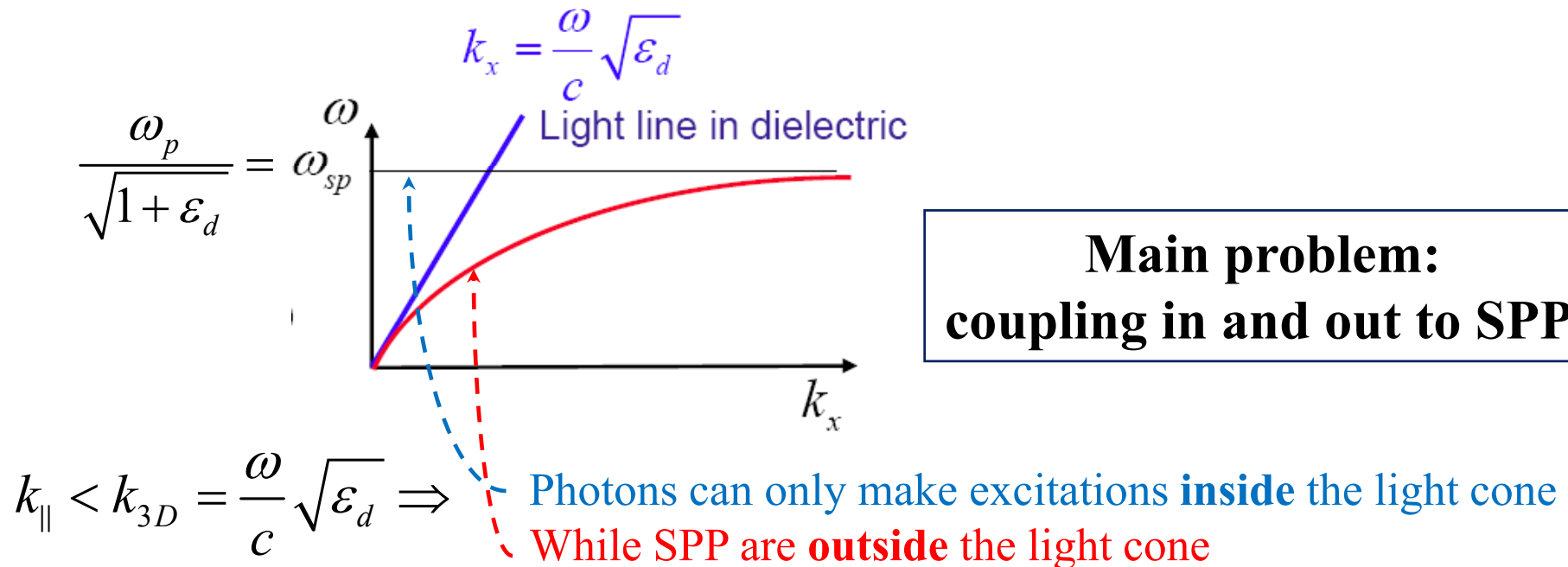
$k_{SPP} (\approx 10 - 100 \mu\text{m}^{-1}) > \omega \sqrt{\epsilon_d} / c \Rightarrow$ **Beyond the diffraction limit**



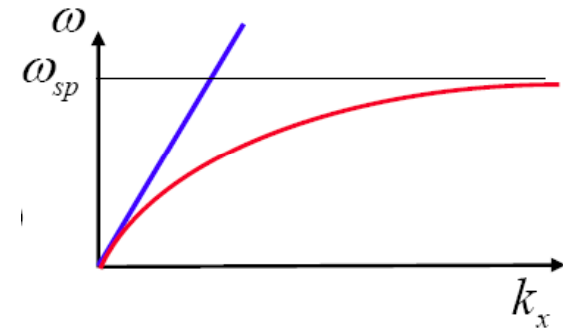
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One problem: coupling light to SPPs



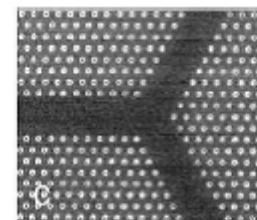
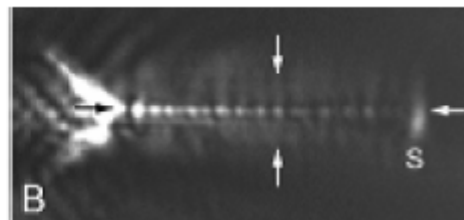
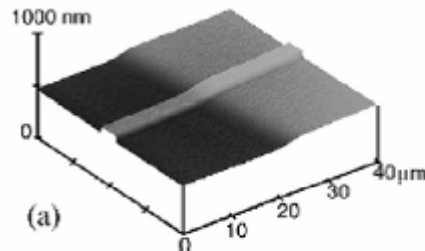
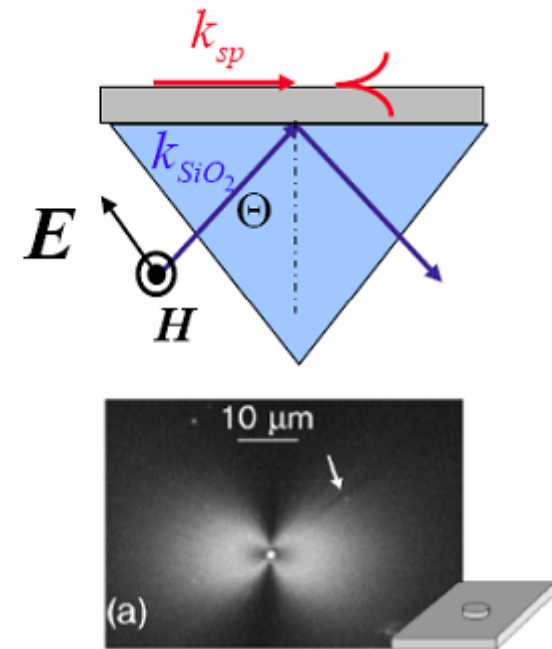
Coupling light to surface plasmon-polaritons

- Using high energy electrons (EELS)

- Kretschman geometry

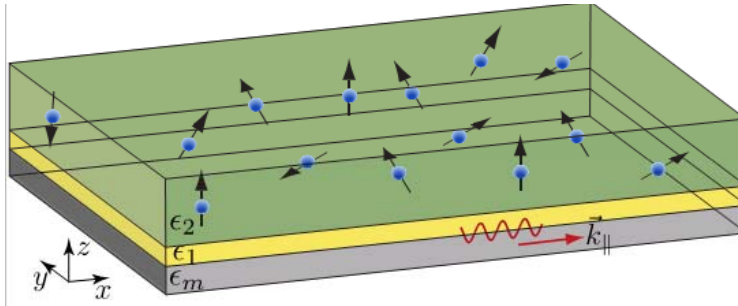
$$k_{||, \text{SiO}_2} = \sqrt{\epsilon_d} \frac{\omega}{c} \sin \theta = k_{sp}$$

- Grating coupling
- Coupling using subwavelength features
- A diversity of guiding geometries



SPP

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Quantization of plasmons (without losses)

Quantization of an electric field $\vec{E}(\vec{r}) = \sum_{\vec{k}} \sqrt{\frac{\hbar\omega(k)}{2\epsilon_0 A}} \vec{u}_{\vec{k}}(z) e^{i(\vec{k}\cdot\vec{\rho} + k_z z)} a_{\vec{k}}$

$$\vec{r} = (\vec{\rho}, z)$$

$$\vec{u}_{\vec{k}}(z) = \frac{1}{\sqrt{L(\vec{k})}} e^{-k_z z} \left(\hat{u}_{\vec{k}} - \frac{|\vec{k}|}{ik_z} \hat{u}_z \right)$$

with

$$L(\omega) = \frac{\pi}{2} \frac{\epsilon_m(\omega) - \epsilon_d}{\sqrt{\epsilon_d \epsilon_m(\omega)} |\vec{k}(\omega)|} \left[\epsilon_m(\omega) + \epsilon_d \left(1 + \omega \frac{d\epsilon_m(\omega)}{d\omega} \right) \right]$$

effective length to normalize the energy of each mode,

$$H_{EM} = \sum_{\vec{k}} \omega(k) a_{\vec{k}}^\dagger a_{\vec{k}}$$

Quantization of modes in a medium with dissipation

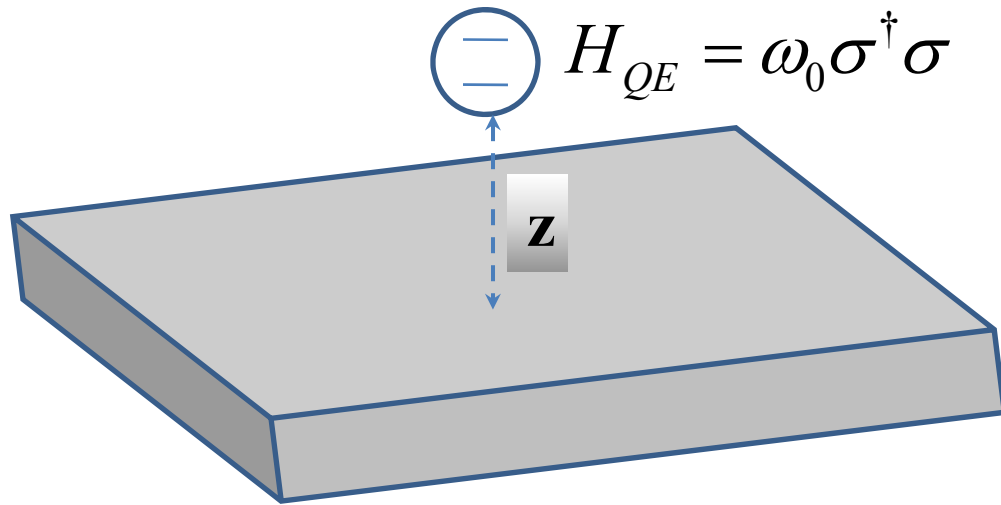
“Quantum Optics “ Vogel & Welsch (Wiley 2006)

$\vec{P}_N(\vec{r}, t)$ **Noise Polarization** associated with absorption

$$\begin{aligned}\vec{P}_N(\vec{r}, \omega) &= i \sqrt{\frac{\hbar \epsilon_0}{\pi}} \operatorname{Im} \varepsilon(\vec{r}, \omega) \vec{f}(\vec{r}, \omega) \\ \vec{E}(\vec{r}, \omega) &= i \sqrt{\frac{\hbar}{\pi \epsilon_0}} \frac{\omega^2}{c^2} \int d\vec{r}' \sqrt{\operatorname{Im} \varepsilon(\vec{r}', \omega)} \hat{G}(\vec{r}, \vec{r}', \omega) \vec{f}(\vec{r}', \omega) \\ \hat{H} &= \int d\vec{r} \int_0^\infty d\omega \hbar \omega \vec{f}^\dagger(\vec{r}, \omega) \vec{f}(\vec{r}, \omega)\end{aligned}$$

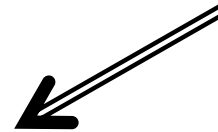
Hereafter, everything is similar to the non-dissipation case with $\vec{f}(\vec{r}, \omega)$ are **bosonic fields** playing the role of $a_{\vec{k}}$

Interaction of 1 quantum emitter (QE) with SPP



Interaction with a dipole

$$U = \int d\vec{r} \vec{\mu}(\vec{r}) \cdot \vec{E}(\vec{r})$$



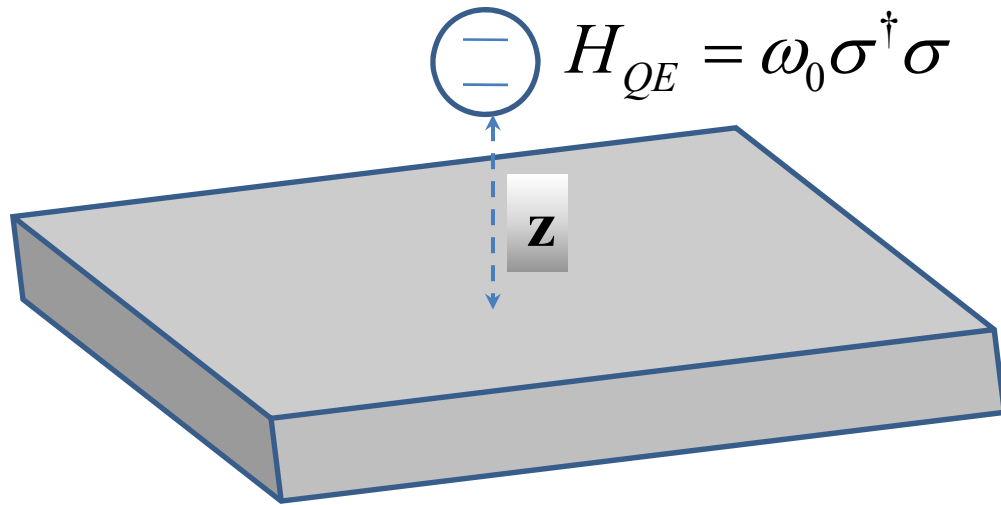
$$H_{int}(t) = \sum_{\vec{k}} \frac{g_{\vec{\mu}}(\vec{k}; z)}{\sqrt{A}} \left(a_{\vec{k}} e^{i(\vec{k} \cdot \vec{r} - \omega(k)t)} + a_{\vec{k}}^\dagger e^{-i(\vec{k} \cdot \vec{r} - \omega(k)t)} \right) \left(\sigma^\dagger e^{i\omega_0 t} + \sigma e^{-i\omega_0 t} \right)$$

$$g_{\vec{\mu}}(\vec{k}; z) = E_{\vec{k}} \vec{\mu} \cdot \vec{u}_{\vec{k}}(z) = \sqrt{\frac{\omega(\vec{k})}{2\epsilon_0 L(\vec{k})}} e^{-k_z z} \vec{\mu} \cdot \left(\hat{u}_{\vec{k}} - \frac{|\vec{k}|}{k_z} \hat{u}_z \right)$$

$$\mu^2 = 3\pi\epsilon_0 c^3 \gamma_0 / \omega_0^3$$

**decay rate
of bare QE**

Interaction of 1 quantum emitter (QE) with SPP



Interaction with a dipole

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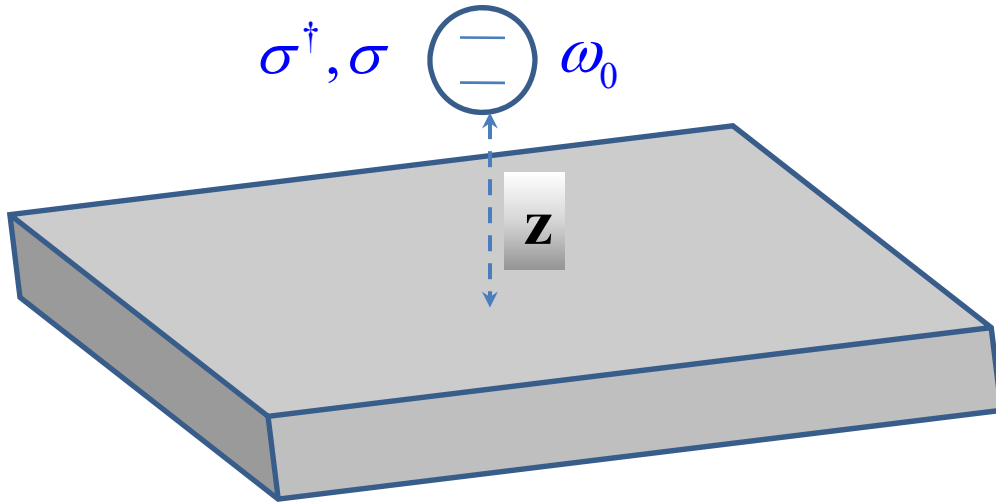
$$\mu^2 = 3\pi\epsilon_0 c^3 \gamma_0 / \omega_0^3$$

decay rate
of bare QE

In RWA

$$H_{int} \approx \sum_{\vec{k}} \frac{g_{\vec{\mu}}(\vec{k}; z)}{\sqrt{A}} \left(a_{\vec{k}} \sigma^\dagger e^{i\vec{k} \cdot \vec{r}} + a_{\vec{k}}^\dagger \sigma e^{-i\vec{k} \cdot \vec{r}} \right)$$

Interaction of 1 quantum emitter (QE) with SPP

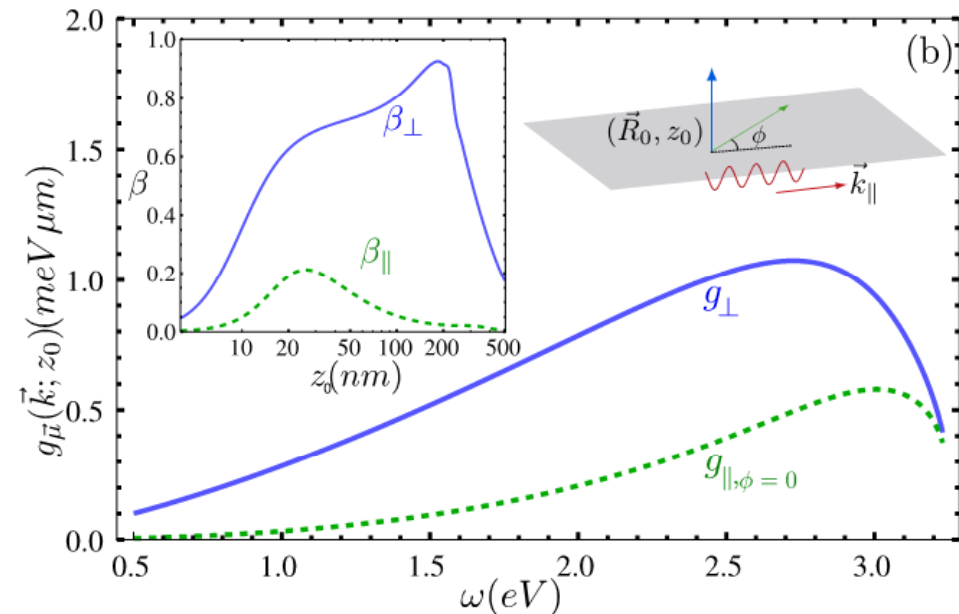


One QE with ω_0 only couples to a bright SPP \equiv symmetric linear comb. (J_0 Bessel funct.) of all the modes with

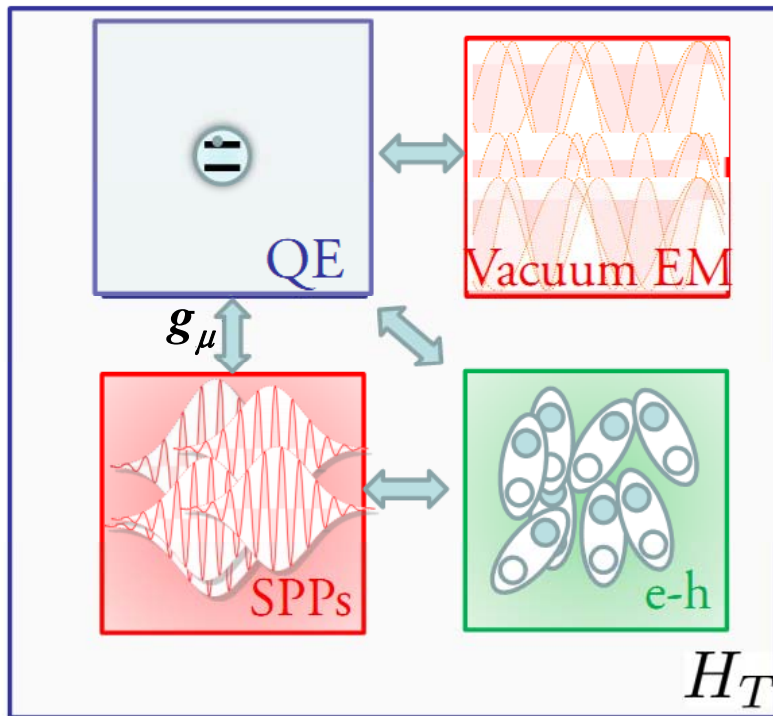
$$|\vec{k}|; \omega_0 = \omega_{SPP}(|\vec{k}|)$$

The higher coupling does not coincide with the higher β -factor

$$\beta = \frac{\text{radiation to plasmons}}{\text{total radiation}} = \frac{\gamma_{pl}}{\gamma}$$

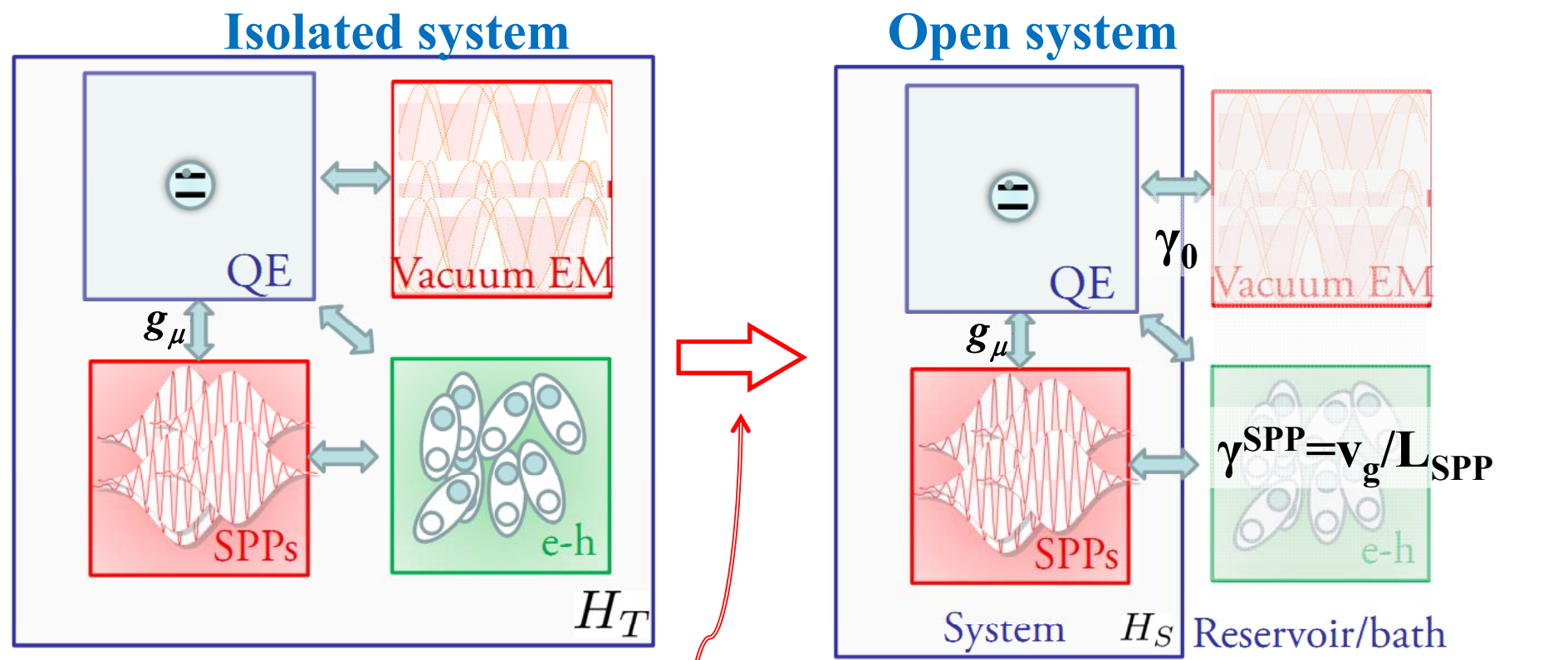


Scheme of the quantum dynamics of an open system



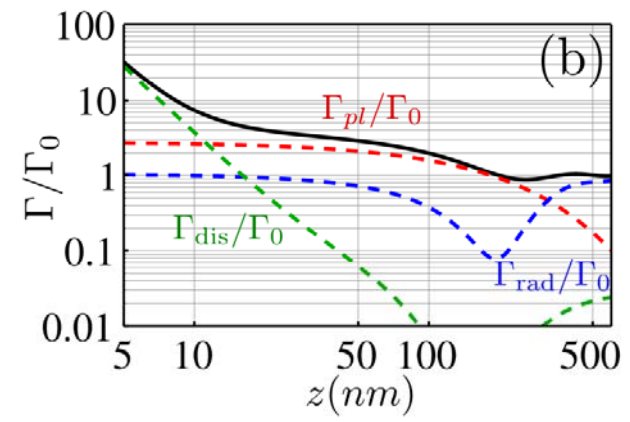
Solving $i \frac{\partial |\Phi_{TOT}\rangle}{\partial t} = H_{TOT} |\Phi_{TOT}\rangle$
is complicated and unnecessary

Scheme of the quantum dynamics of an open system

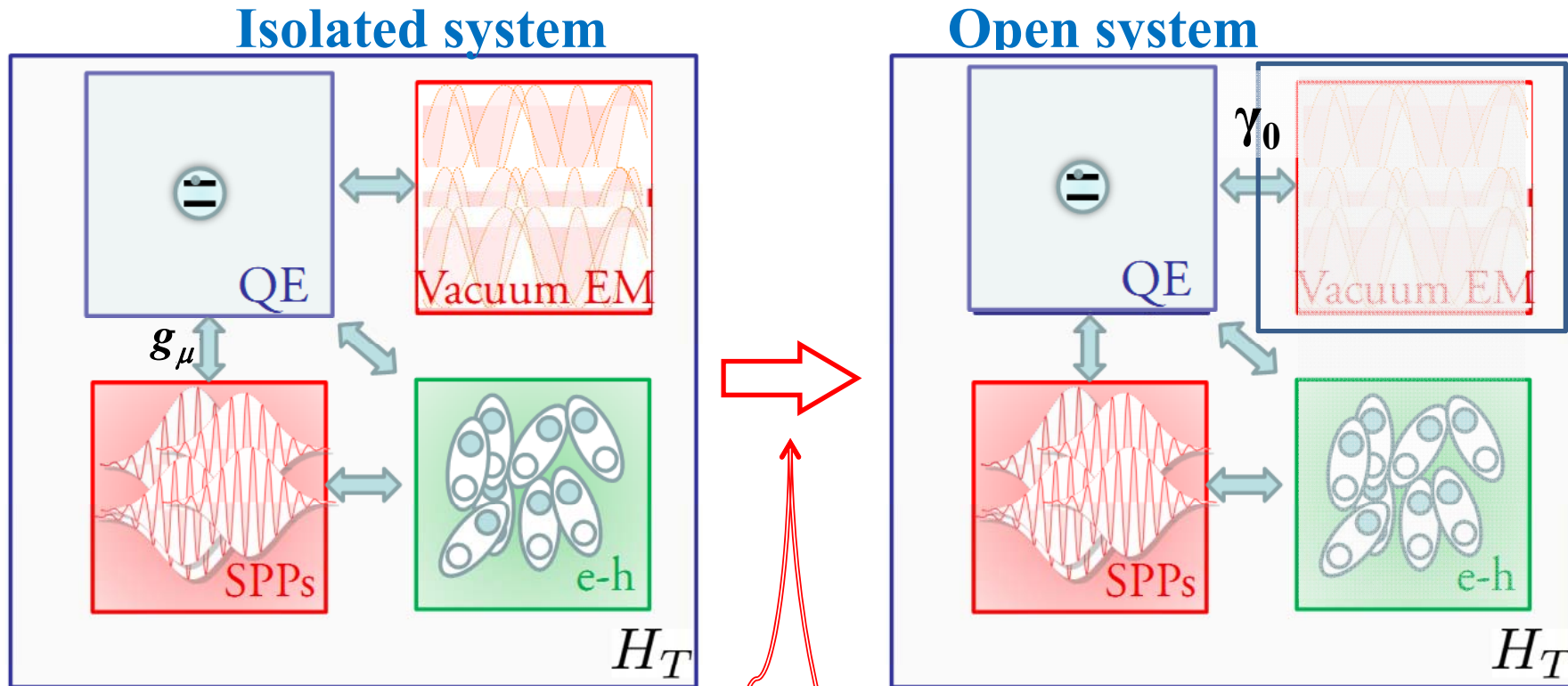


Solving $i \frac{\partial |\Phi_{TOT}\rangle}{\partial t} = H_{TOT} |\Phi_{TOT}\rangle$
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Tracing out the reservoir's
degrees of freedom

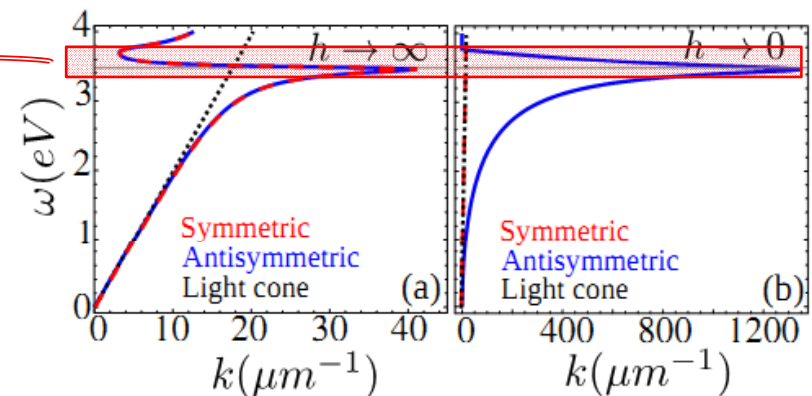


Scheme of the quantum dynamics of an open system



Solving $i \frac{\partial |\Phi_{TOT}\rangle}{\partial t} = H_{TOT} |\Phi_{TOT}\rangle$
 is complicated and unnecessary

When dissipation at the metal is very high,
 tracing out **ONLY** the vacuum's degrees of
 freedom

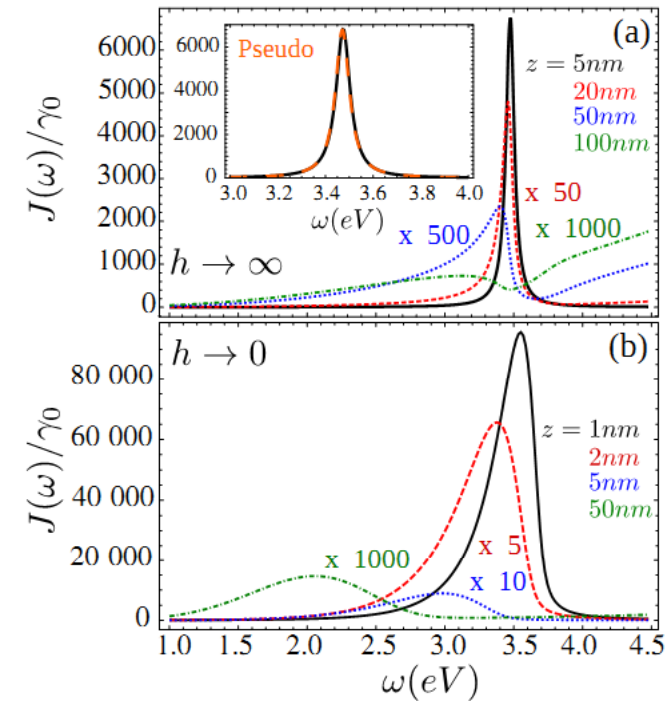
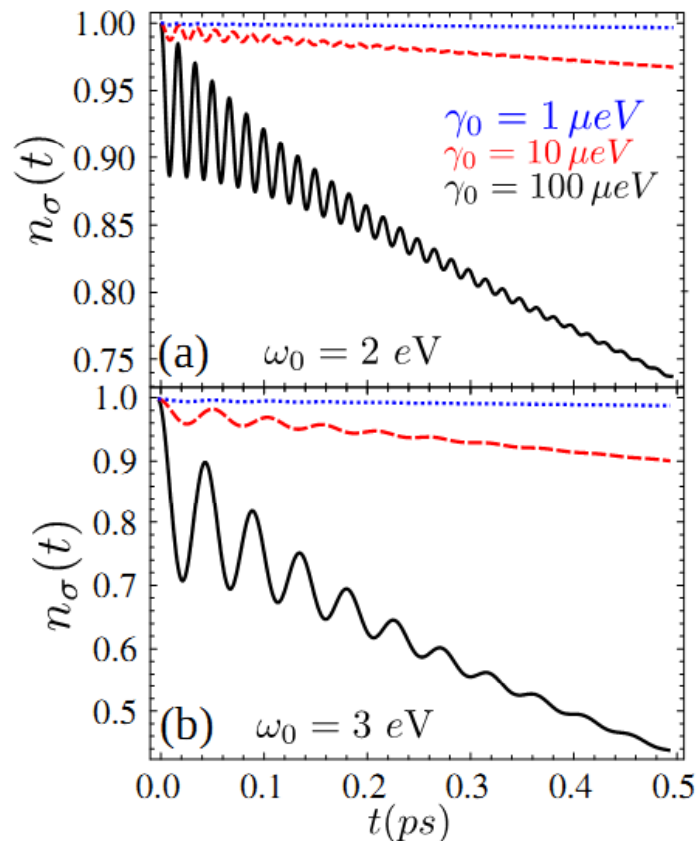


Dynamics of the QE population: Weisskopf-Wigner

$$\dot{c}_\sigma(t) = -\int_0^t K_{\vec{\mu}}(t-\tau; z) c_\sigma(\tau) d\tau - \gamma_0 c_\sigma(t) / 2 \quad ; \quad c_\sigma(0) = 1$$

$$K_{\vec{\mu}}(\tau; z) = \sum_{\vec{k}} |g_{\vec{\mu}}(\vec{k}; z)|^2 e^{i[\omega_0 - \omega(\vec{k})]\tau} = \int_0^{\omega_c} d\omega J(\omega; z) e^{i(\omega_0 - \omega)\tau}$$

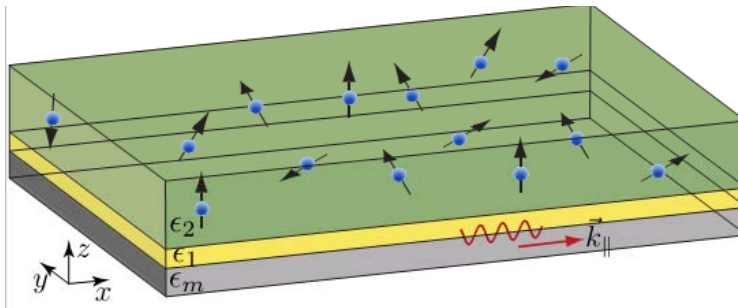
$$J(\omega; z) = \frac{1}{\pi \epsilon_n} \vec{\mu} \left[\frac{\omega^2}{c^2} \text{Im}[\hat{G}(\vec{r}_0, \vec{r}_0, \omega)] \right] \vec{\mu} = g^2(\omega) \rho(\omega)$$



- For a single QE with ω_0 around the cut-off, spectral density (J) has a non lorentzian shape \Rightarrow different dynamics that a pseudomode (cavity QED) !
- **Non-markovian noise**
- Height/width ratio of J determines/allows some (fast & local) reversibility !

SPP

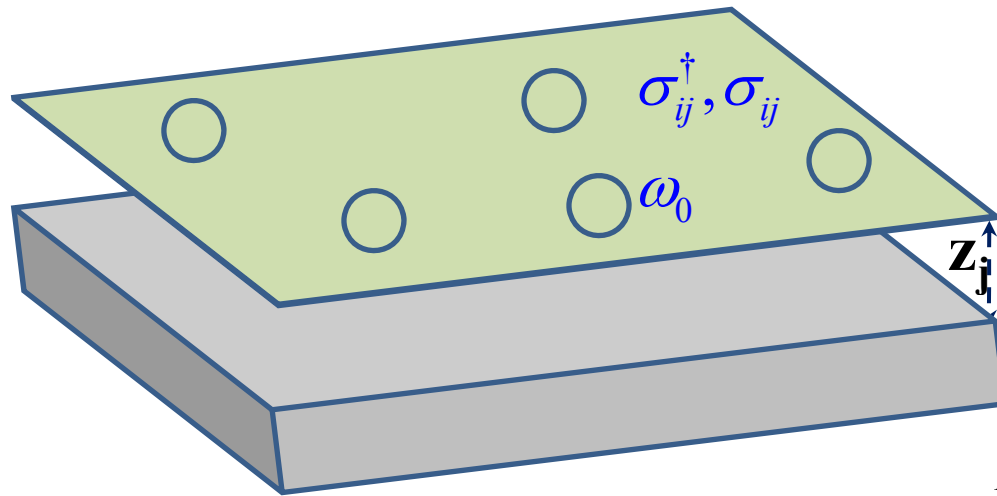
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Exciton collective mode of emitters in a plane



More complicated system:
Dynamics described by
master eq. for density matrix
& quantum regression th.

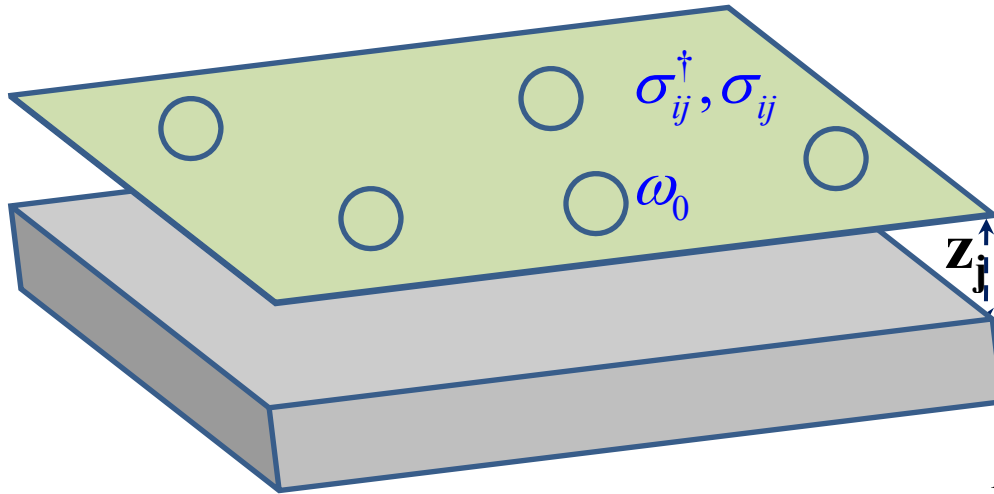
$$H_0^N + H_{pl} = \sum_{i=1}^{N_s} \omega_0 \sigma_{i,j}^\dagger \sigma_{i,j} + \sum_{\vec{k}} \omega(\vec{k}) a_{\vec{k}}^\dagger a_{\vec{k}}$$

$$H_{int}^N = \sum_{\vec{k}} \sum_{i=1}^{N_s} \frac{g_{\vec{\mu}}(\vec{k}; z_j)}{\sqrt{A}} (a_{\vec{k}}^\dagger \sigma_{i,j} e^{i\vec{k} \cdot \vec{r}_i} + a_{\vec{k}}^\dagger \sigma_{i,j} e^{-i\vec{k} \cdot \vec{r}_i})$$

$$g_{\vec{\mu}}(\vec{k}; z_j) = \sqrt{\frac{\omega(\vec{k})}{2\epsilon_0 L(\vec{k})}} e^{-k_z z_j} \vec{\mu} \cdot \left(\hat{u}_{\vec{k}} - \frac{|\vec{k}|}{k_z} \hat{u}_z \right)$$

No fitting !!!

Exciton collective mode of emitters in a plane



Holstein-Primakoff transf.
(low excitation \Rightarrow no saturation)
& Collective bosonic mode



$$\sigma_{i,j}^\dagger = \sqrt{1 - b_{i,j}^\dagger b_{i,j}} \cdot b_{i,j} \approx b_{i,j}^\dagger$$

$$D_j^\dagger(\vec{q}) = \frac{1}{\sqrt{N_s}} \sum_{i=1}^{N_s} b_{i,j}^\dagger e^{i\vec{q} \cdot \vec{R}_i}$$

$$b_{i,j}^\dagger = \frac{1}{\sqrt{N_s}} \sum_{\vec{q}} D_{j,\vec{q}}^\dagger e^{-i\vec{q} \cdot \vec{R}_i}$$

**More complicated system:
Dynamics described by
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$$H_0^N + H_{pl} = \sum_{i=1}^{N_s} \omega_0 \sigma_{i,j}^\dagger \sigma_{i,j} + \sum_{\vec{k}} \omega(\vec{k}) a_{\vec{k}}^\dagger a_{\vec{k}}$$

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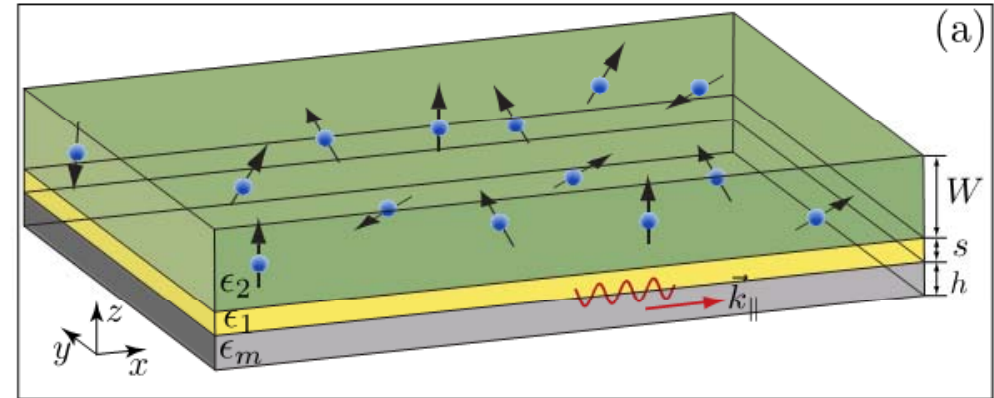
No fitting !!!

$$H_{int} = \sum_{\vec{k}, \vec{q}} \sum_{i=1}^{N_s} \frac{g_{\vec{\mu}}(\vec{k}; z_j) \sqrt{n_s}}{N_s} (S(\vec{k} - \vec{q}) \cdot \vec{r}_i a_{\vec{k}}^\dagger D_j^\dagger(\vec{q}) + S^*(\vec{k} - \vec{q}) \cdot \vec{r}_i a_{\vec{k}}^\dagger D_j(\vec{q}))$$

$$S(\vec{k}) = \frac{1}{N_s} \sum_{i=1}^{N_s} e^{i\vec{k} \cdot \vec{r}_i} \quad \text{Structure factor}$$

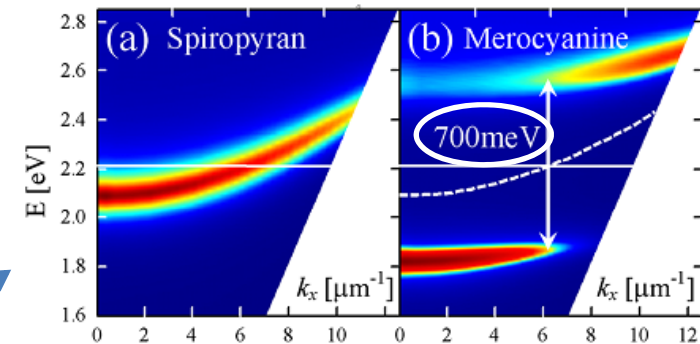
Experimental evidence of strong coupling of SPP & excitons

QE are not just in a plane



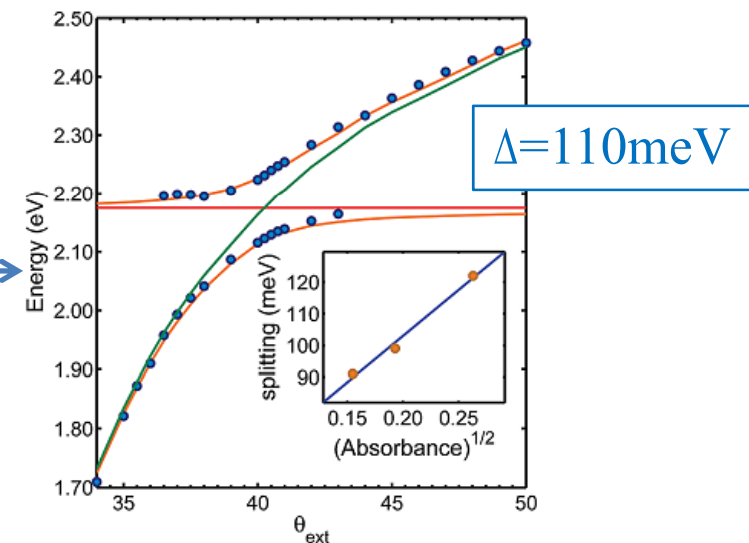
Ensembles of organic molecules

- J. Bellessa, et al, Phys. Rev. Lett. 93, 036404 (2004).
- J. Dintinger, et al, Phys. Rev. B 71, 035424 (2005).
- T. K. Hakala, et al, Phys. Rev. Lett. 103, 053602 (2009).
- P. Vasa, et al, Nano Lett. 12, 7559 (2010).
- T. Schwartz, et al, Phys. Rev. Lett. 106, 196405 (2011).

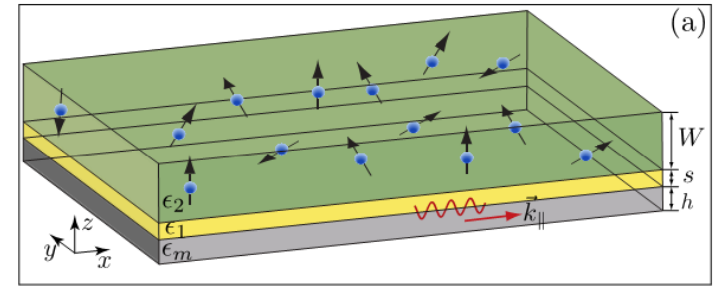


Semicond. nanocrystals & Quantum wells

- P. Vasa, et al., Phys. Rev. Lett. 101, 116801 (2008).
- J. Bellessa, et al, Phys. Rev. B 78 (2008).
- D. E. Gomez, et al, Nano Lett. 10, 274 (2010).
- M. Geiser, et al, Phys. Rev. Lett. 108, 106402 (2012).



Excitonic collective mode in the volume of width W



Coupling depends on distance z_j

$g_{\bar{\mu}}(\vec{k}; z_j) \Rightarrow$ **More complicated collective mode**

For many QE with disorder $S(\vec{k} - \vec{q}) \approx \delta_{\vec{k},0}$ momentum is conserved

Average of random orientations

$$H_{\text{int}} = \sum_{\vec{k}} \sum_{j=1}^{N_L} g_{\bar{\mu}}(\vec{k}; z_j) \sqrt{n_s} (a_{\vec{k}} D_j^\dagger(\vec{k}) + a_{\vec{k}}^\dagger D_j(\vec{k}))$$

$$D^\dagger(\vec{k}) = \frac{1}{g_{\bar{\mu}}^N(\vec{k})} \sum_{j=1}^{N_L} g_{\bar{\mu}}(\vec{k}; z_j) D_j^\dagger(\vec{k}) \quad ; \quad [D_i(\vec{k}), D_j^\dagger(\vec{k})] = \delta_{ij}$$

$$g_{\bar{\mu}}^N(\vec{k}) = \sqrt{\sum_{j=1}^{N_L} |g_{\bar{\mu}}(\vec{k}, z_j)|^2} \rightarrow \sqrt{n \int_s^{s+W} dz |g_{\bar{\mu}}(\vec{k}, z)|^2}$$

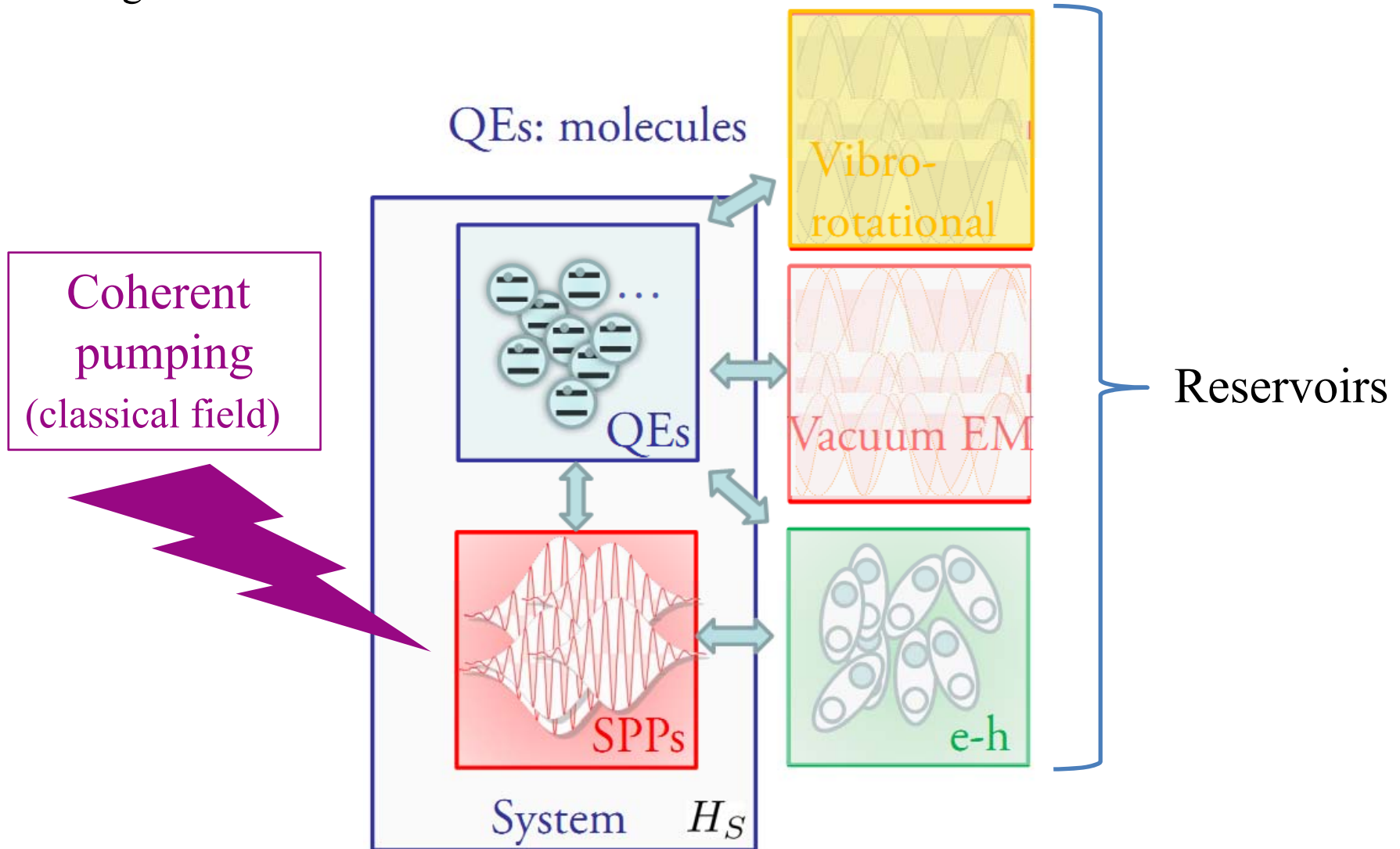
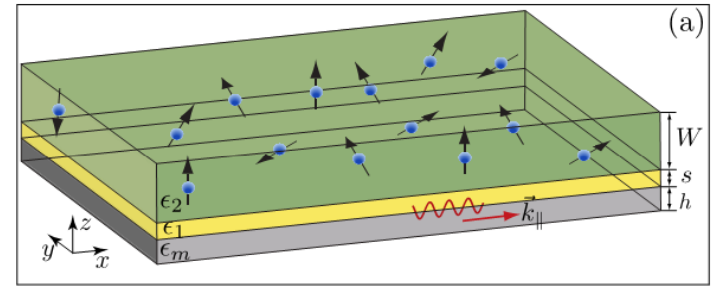
$$H_{\vec{k}}^N = \omega_0 D^\dagger(\vec{k}) D(\vec{k}) + \omega_{\vec{k}} a^\dagger(\vec{k}) a(\vec{k}) + g_{\bar{\mu}}^N(\vec{k}) (a(\vec{k}) D^\dagger(\vec{k}) + a^\dagger(\vec{k}) D(\vec{k}))$$

No fitting !

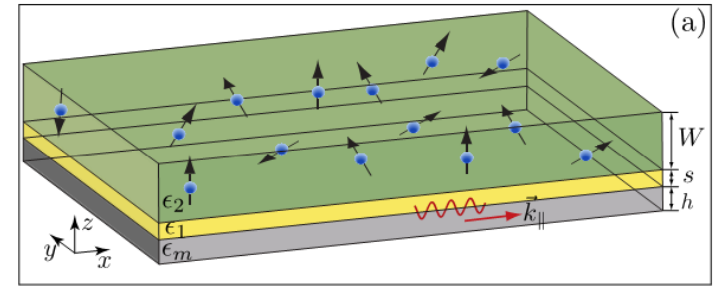
Decay of the collective mode $\gamma_{D_{\vec{k}}} = \frac{n}{|g_{\bar{\mu}}^N(\vec{k})|^2} \int_s^{s+W} dz \gamma_\sigma(z) |g_{\bar{\mu}}(\vec{k}, z)|^2$

Dynamics under coherent pumping of a SPP with k-vector

Average of random orientations



Dynamics under coherent pumping of a SPP with k-vector



$$H_{\vec{k}}^N = \omega_0 D^\dagger(\vec{k}) D(\vec{k}) + \omega_{\vec{k}} a^\dagger(\vec{k}) a(\vec{k}) + g_{\vec{\mu}}^N(\vec{k}) (a(\vec{k}) D^\dagger(\vec{k}) + a^\dagger(\vec{k}) D(\vec{k}))$$

$$H_{\vec{k}}^L(t) = \Omega_{\vec{k}} (a_{\vec{k}} e^{i\omega_L t} + a_{\vec{k}}^\dagger e^{-i\omega_L t})$$

$$\dot{\rho}_{\vec{k}} = i[\rho_{\vec{k}}, H_{\vec{k}}^N + H_{\vec{k}}^L] + \frac{\gamma_{D_{\vec{k}}}}{2} \mathcal{L}_{D_{\vec{k}}} + \frac{\gamma_{a_{\vec{k}}}}{2} \mathcal{L}_{a_{\vec{k}}} + \frac{\gamma_{\phi}}{2} \mathcal{L}_{D_{\vec{k}}^\dagger D_{\vec{k}}}$$

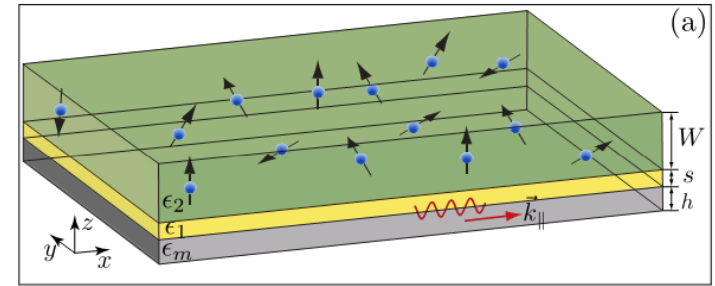
Exciton
decay

Plasmon
decay

Pure dephasing
(vibro-rotation)

$$\mathcal{L}_c = (2c\rho c^\dagger - c^\dagger c\rho - \rho c^\dagger c)$$

Dynamics under coherent pumping of a SPP with k-vector



$$H_{\vec{k}}^N = \omega_0 D^\dagger(\vec{k}) D(\vec{k}) + \omega_{\vec{k}} a^\dagger(\vec{k}) a(\vec{k}) + g_{\vec{\mu}}^N(\vec{k}) (a(\vec{k}) D^\dagger(\vec{k}) + a^\dagger(\vec{k}) D(\vec{k}))$$

$$H_{\vec{k}}^L(t) = \Omega_{\vec{k}} (a_{\vec{k}} e^{i\omega_L t} + a_{\vec{k}}^\dagger e^{-i\omega_L t})$$

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Exciton
decay

Plasmon
decay

Pure dephasing
(vibro-rotation)

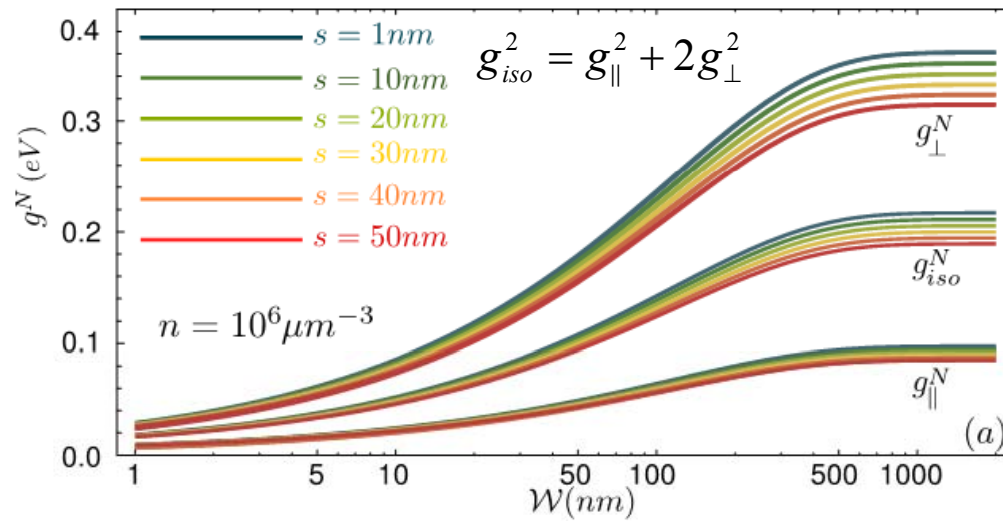
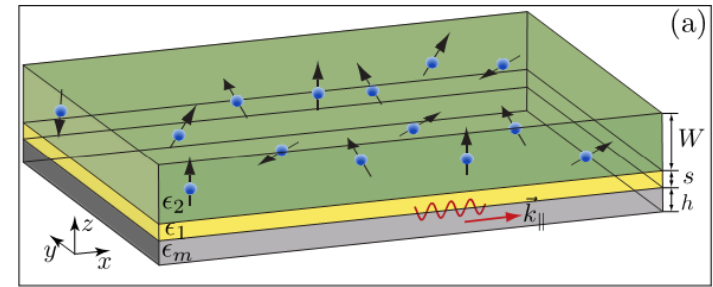
$$\mathcal{L}_c = (2c\rho c^\dagger - c^\dagger c \rho - \rho c^\dagger c)$$

At the crossing (k_0) between exciton and SPP,
Rabi splitting is analytical

$$R = \sqrt{[g_{\vec{\mu}}^N(\vec{k}_0)]^2 - (\gamma_{D_{\vec{k}_0}} + \gamma_{\phi} - \gamma_{a_{\vec{k}_0}})^2 / 4} \quad \text{with } [g_{\vec{\mu}}^N(\vec{k}_0)]^2 \propto n$$

Strong coupling between SPP & excitons

$$\gamma_0 = 0.1 \text{ meV}$$

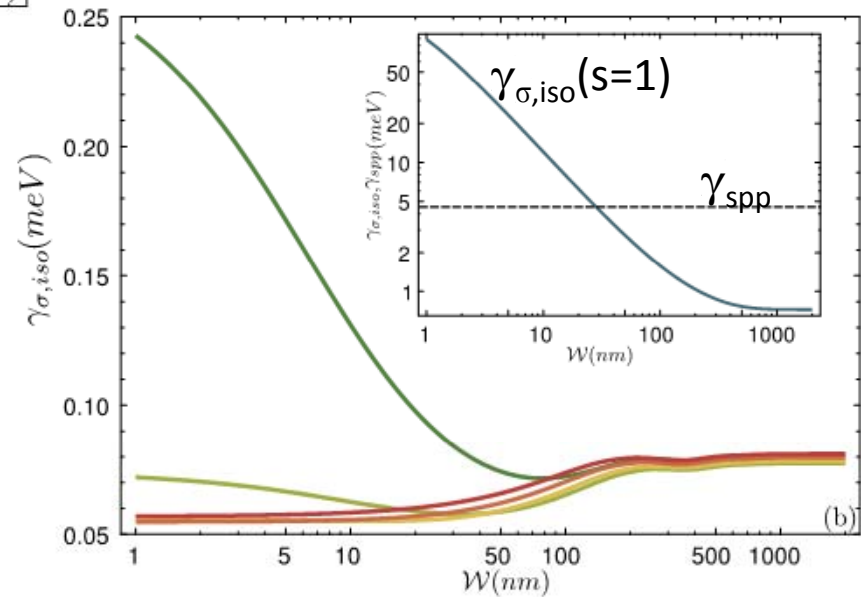


- g^N depends on W with saturation due to SPP z-decay
- g^N practically independ. on s

$$\Omega_{\vec{k}} = 0.1 g^N$$

$$n = 10^6 \mu\text{m}^{-3}$$

$$\omega_0 = 2 \text{ eV}$$



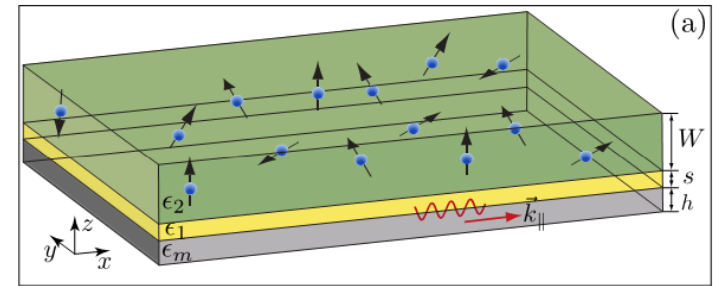
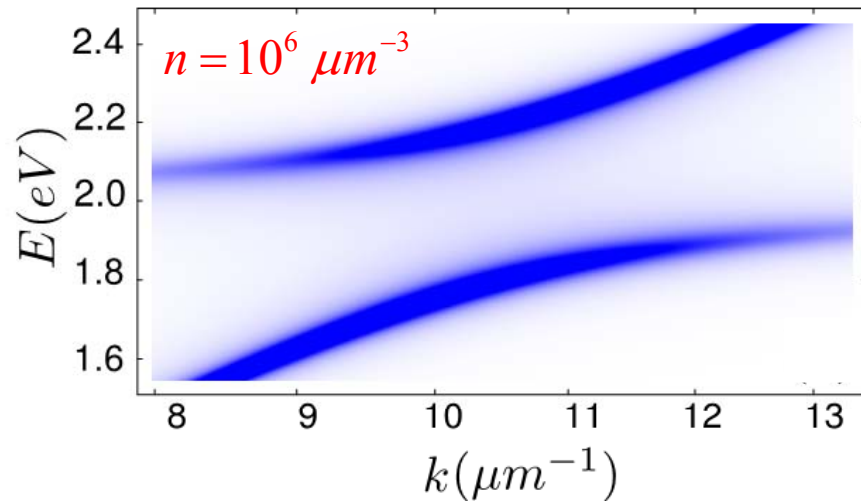
Strong coupling between SPP & excitons

$$s = 1 \text{ nm} ; W = 500 \text{ nm}$$

$$\omega_0 = 2 \text{ eV} ; \Omega_{\vec{k}} = 0.1 g^N \text{ (40 meV)}$$

$$\gamma_0 = 0.1 \text{ meV} ; \gamma_\phi = 0.1 g^N \text{ (RT)}$$

Polariton populations \propto absorption spect.



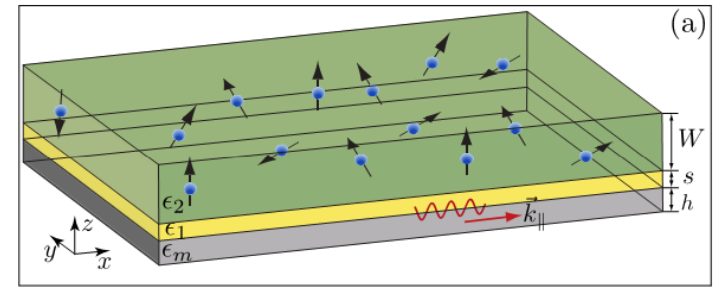
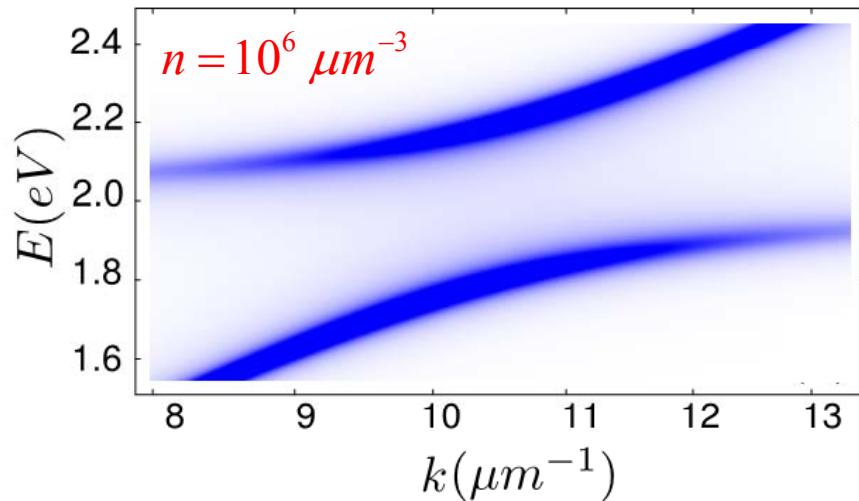
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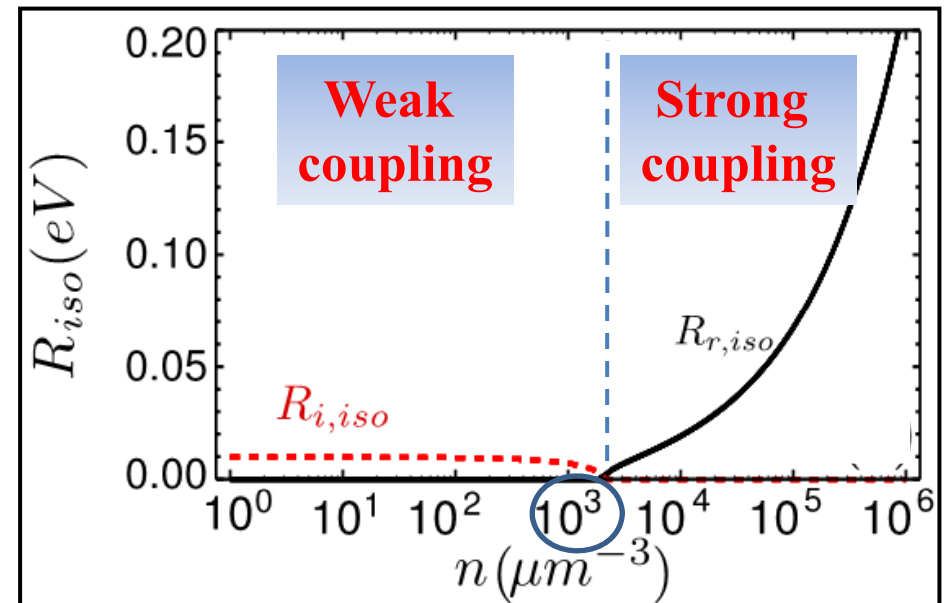
$$\gamma_0 = 0.1 \text{ meV} ; \gamma_\phi = 0.1 g^N \text{ (RT)}$$

Polariton populations \propto absorption spect.



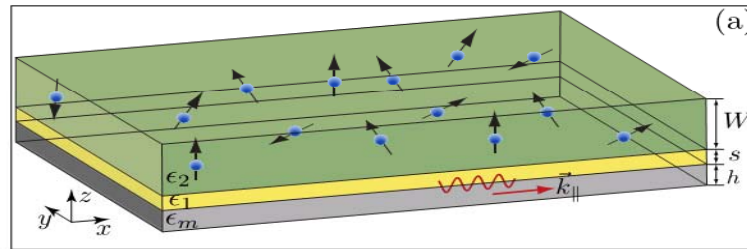
Rabi splitting (at k_0)

$$R = \sqrt{[g_{\vec{\mu}}^N(\vec{k}_0)]^2 - (\gamma_{D_{\vec{k}_0}} + \gamma_\phi - \gamma_{a_{\vec{k}_0}})^2 / 4} ; [g_{\vec{\mu}}^N(\vec{k}_0)]^2 \propto n$$



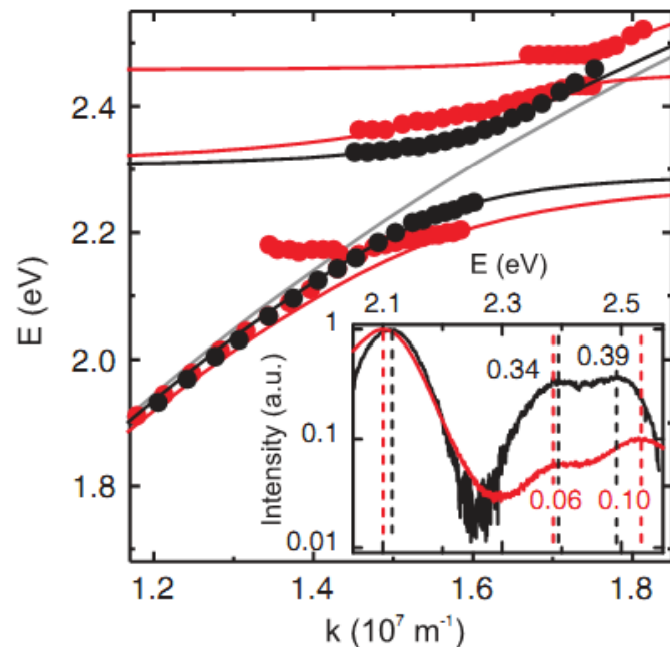
At RT, the incoherent processes (γ_ϕ) determine a critical density for observing strong coupling

Strong coupling between SPP & excitons: comparison with experiments



Experiment

Hakala et al. PRL, 103, 053602 (09)



Our theory

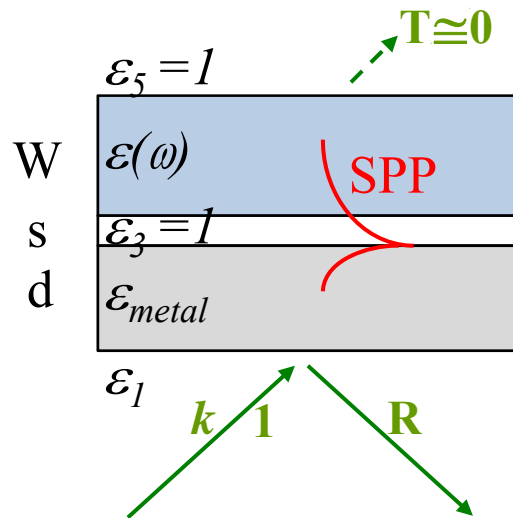
$$W = 50\text{nm}; n = 1.2 \times 10^8 \mu\text{m}^{-3}; \gamma_0 = 1\mu\text{eV}$$

$$R_{th}^{\parallel} = 40\text{meV}, \quad R_{th}^{\perp} = 180\text{meV}, \quad R_{th}^{iso} = 100\text{meV}$$

$$R_{exp} = 115\text{meV}$$

Quantum effects? : (Semi)-classical description

Polarizability of 1 emitter $\alpha(\omega) = \frac{f_0 e^2 / m}{\omega_0^2 - \omega^2 - i\omega\gamma}$; $\epsilon(\omega) = \frac{1 + (2/3)N\alpha(\omega)}{1 - (1/3)N\alpha(\omega)}$ Eff. dielectric
 funct. of emitters



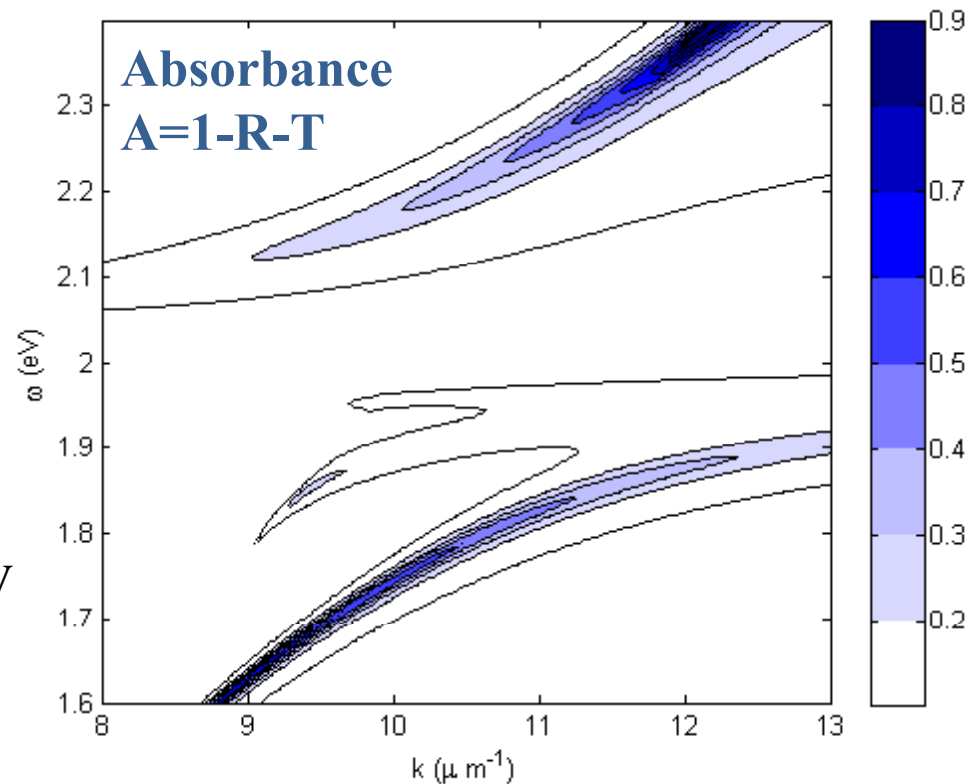
Oscillator strength
 from microscopic info.

$$f_0 = \frac{2m\omega_0}{3e^2\hbar} |\bar{\mu}|^2 = \frac{2\pi m}{e^2} \frac{\epsilon_0 c^3}{\omega_0^2} \gamma_0$$

$\epsilon_1=3$; $d=50\text{nm}$; $s=1\text{nm}$; $W=500\text{nm}$

$\omega_0=2\text{eV}$; $N=10^6 \mu\text{m}^{-3}$

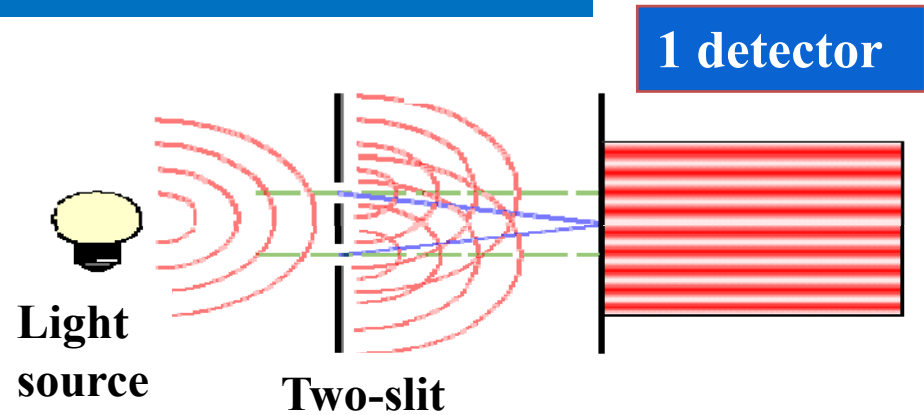
$\gamma = \gamma_0 + \gamma_{deph}$; $\gamma_0=0.1\text{meV}$; $\gamma_{deph}=40\text{meV}$



Quantum effects: 1st & 2nd order coherences

Young's interfer. exp.

$$g^{(1)}(t,0) \propto \langle E^{(-)}(t)E^{(+)}(t) \rangle \propto \langle I(t) \rangle$$



Amplitude interference pattern: the Fouriertransform is the spectrum

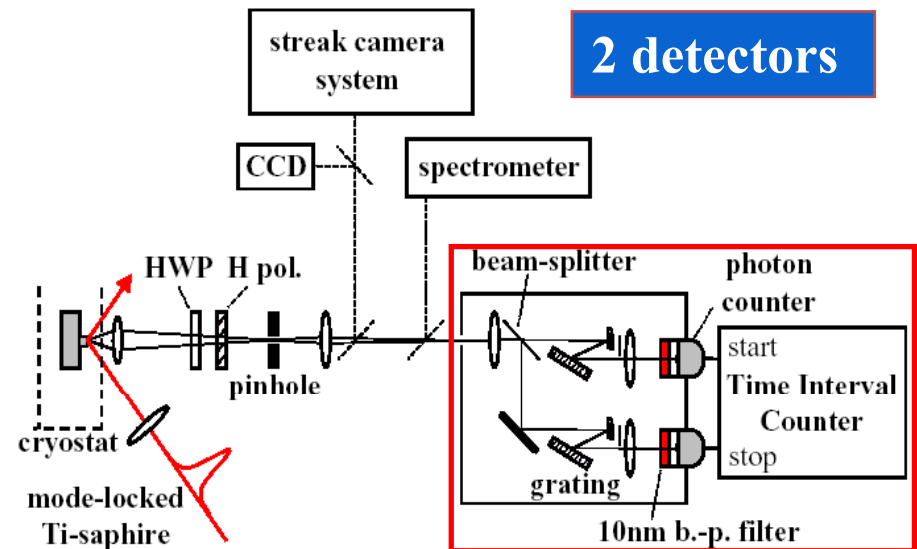
$g^{(1)}$ does not distinguish between classical & quantum light

Hanbury-Brown Twiss exp.

$$g^{(2)}(t,\tau) \propto \langle E^{(-)}(t)E^{(-)}(t+\tau)E^{(+)}(t+\tau)E^{(+)}(t) \rangle$$

$$\propto \langle I(t)I(t+\tau) \rangle$$

Intensity-intensity correlations



Quantum effects: 1st & 2nd order coherences

$$g^{(1)}(t, \tau) \propto \langle E^{(-)}(t) E^{(+)}(t + \tau) \rangle \quad \left\| \quad S(r, \omega) = \frac{1}{\pi} \Re \int_0^{\infty} d\tau \langle E^{(-)}(r, t) E^{(+)}(r, t + \tau) \rangle e^{i\omega\tau} \right.$$

*Spectrum ($g^{(1)}$) \Leftrightarrow Amplitude interf. \oplus 1 measurement
It does not distinguish between classical & quantum waves*

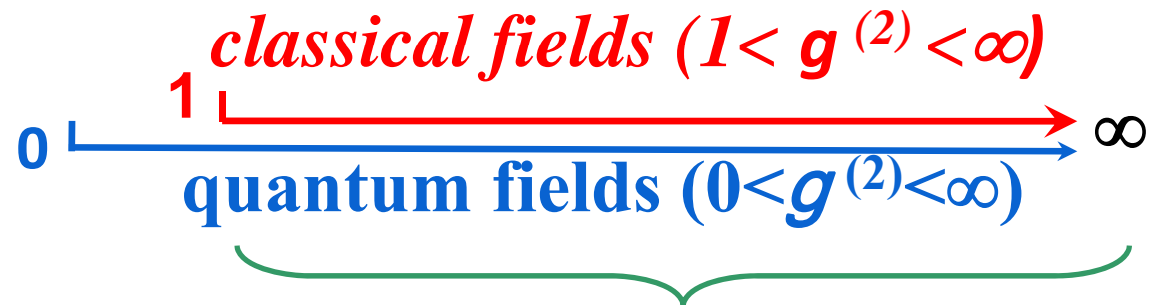
$$g^{(2)}(t, \tau) \propto \langle E^{(-)}(t) E^{(-)}(t + \tau) E^{(+)}(t + \tau) E^{(+)}(t) \rangle \propto \langle I(t) I(t + \tau) \rangle$$

Intensity-int. correlations ($g^{(2)}$) \Leftrightarrow 2 measurements

Classical: First detection does not affect second detection

Quantum: First detection affects second detection

**$g^{(2)}$ can distinguish
between**



(Better to measure Bell's inequalities)

Quantum effects: $g^{(2)}(0)$ in different regimes

BOSONS

Thermal (gaussian)
mixture

Laser threshold $\pi/2$

Poisson distribution
(Coherent sts.)

Sub-poissonian distr.



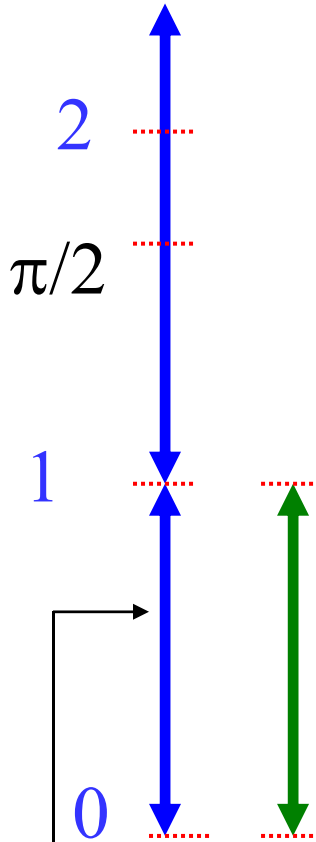
non-classical sts.

For a number (N) st.,
 $g^{(2)}(\tau=0) = 1 - 1/N$

FERMIONS

Poisson distribution
(Coherent sts.)

Chaotic



Quantum effects in the coupling between SPP & excitons

Quantum effects appear when non-linear effects are important: Holstein-Primakoff up to 2nd order

$$\sigma_{i,j} = \sqrt{1 - b_{i,j}^\dagger b_{i,j}} \cdot b_{i,j} \approx (1 - b_{i,j}^\dagger b_{i,j} / 2) b_{i,j}$$

Free energy part of the Hamilt.

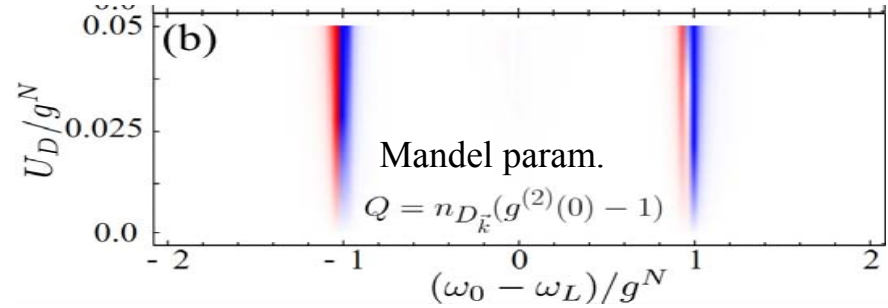
$$H_0^N = \sum_{j=1}^{N_L} \sum_{i=1}^{N_s} \omega_0 b_{i,j}^\dagger b_{i,j} - \sum_{j=1}^{N_L} \sum_{i=1}^{N_s} \omega_0 b_{i,j}^\dagger b_{i,j}^\dagger b_{i,j} b_{i,j}$$

In the quasi-2D limit & using The collective operators:

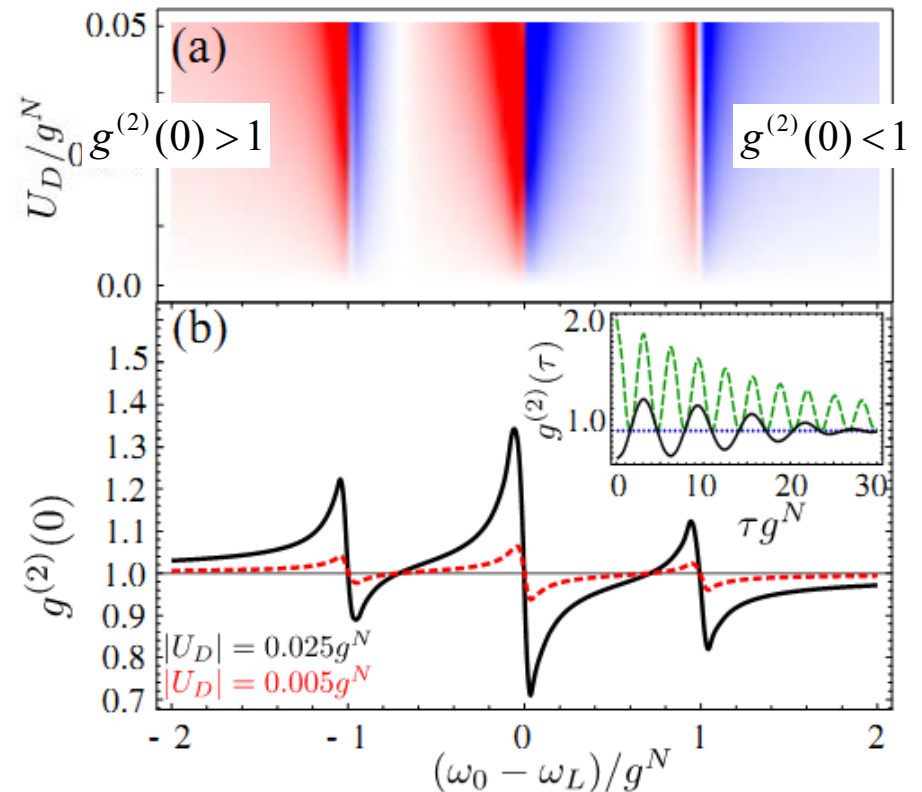
$$H_{nl} = U_D \sum_{\bar{k}, \bar{k}', \bar{q}} D_{\bar{k}+\bar{q}}^\dagger D_{\bar{k}'-\bar{q}}^\dagger D_{\bar{k}} D_{\bar{k}'}$$

$$U_D = -\frac{\omega_0}{N}$$

$$g^{(2)}(\tau) = \lim_{t \rightarrow \infty} \frac{\langle D_{\bar{k}}^\dagger(t) (D_{\bar{k}}^\dagger D_{\bar{k}})(t+\tau) D_{\bar{k}}(t) \rangle}{\langle D_{\bar{k}}^\dagger D_{\bar{k}}(t)^2 \rangle}$$

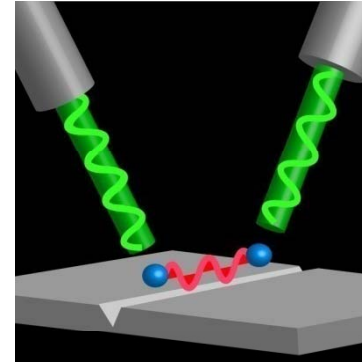


Coherent pumping of plasmons & $\gamma_\phi = 0$



SPP

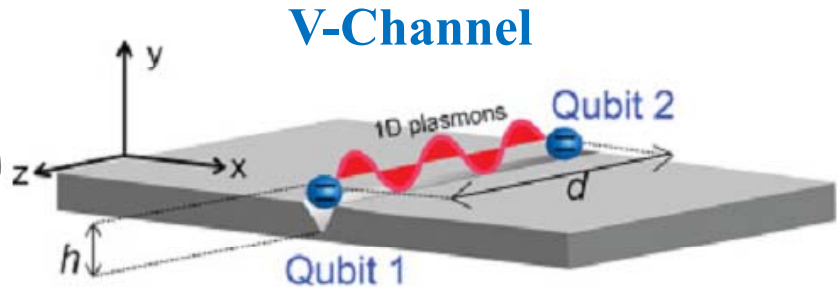
Intermediary for quantum entanglement



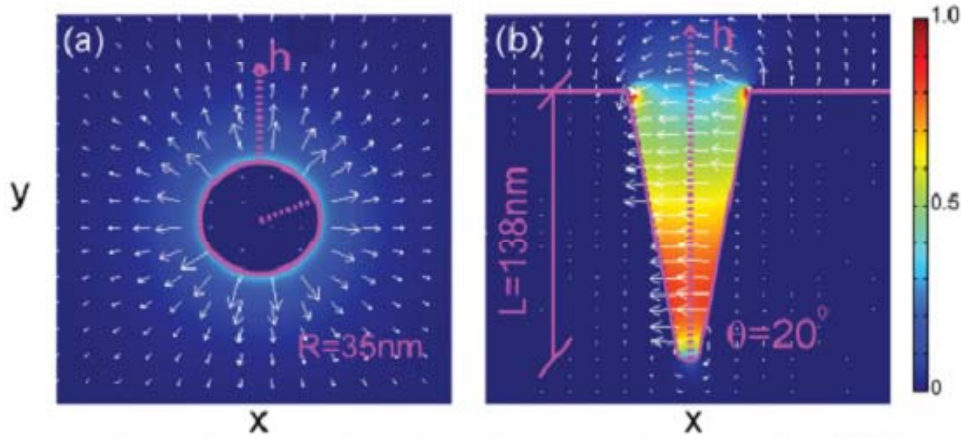
Outline

- Introduction to surface plasmon polaritons (SPP)
- Coupling of 1 quantum emitter (QE) to SPP
- Collective mode (excitons) strongly coupled to SPP
- **Coupling & entanglement of 2 QE mediated by SPP**
- Conclusion

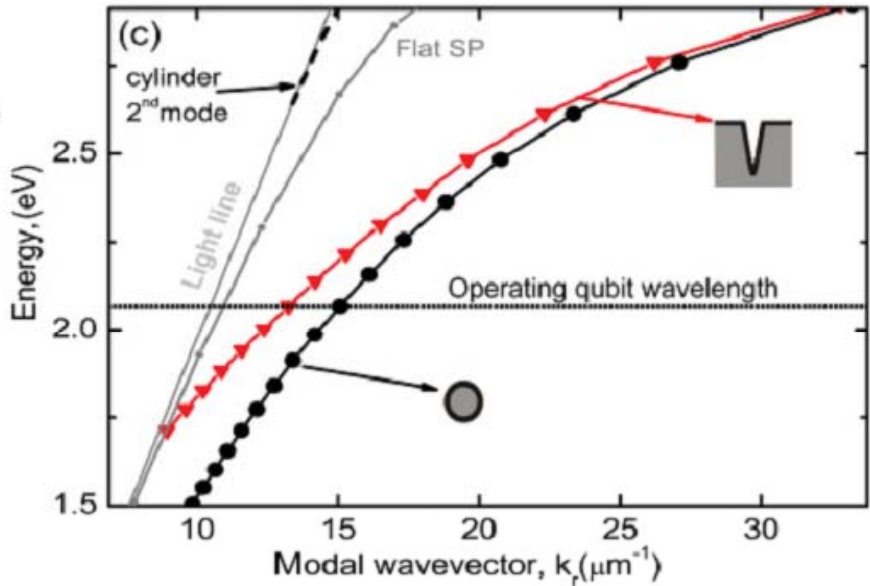
QE-QE coupling mediated by plasmonic waveguides



Waveguide to reinforce QE-QE effects



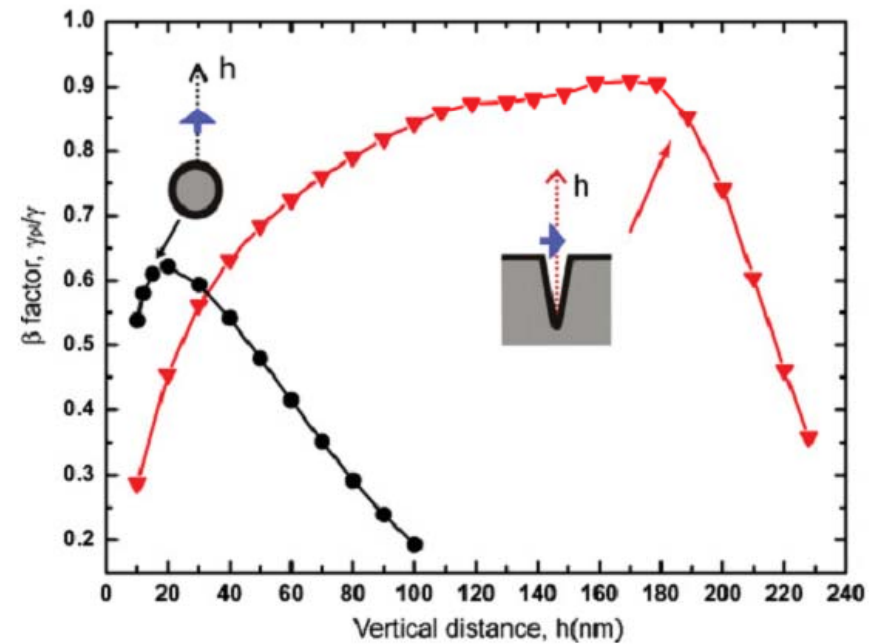
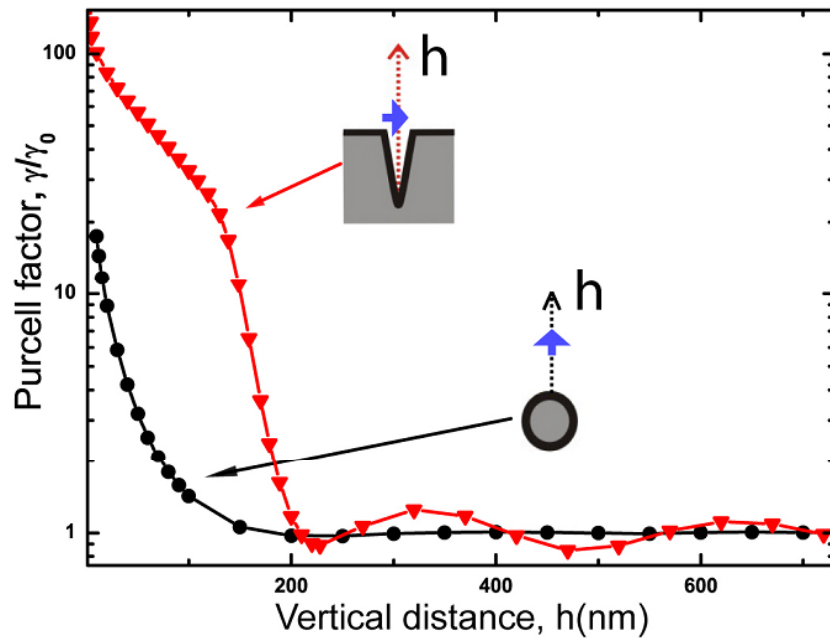
Fields are stronger in the channel than in the cylinder



1QE: β and Purcell factors

Metallic nanostructures increase the emission from a QE (Purcell)
but,
Is it always a coherent emission of SPP's??? (β)

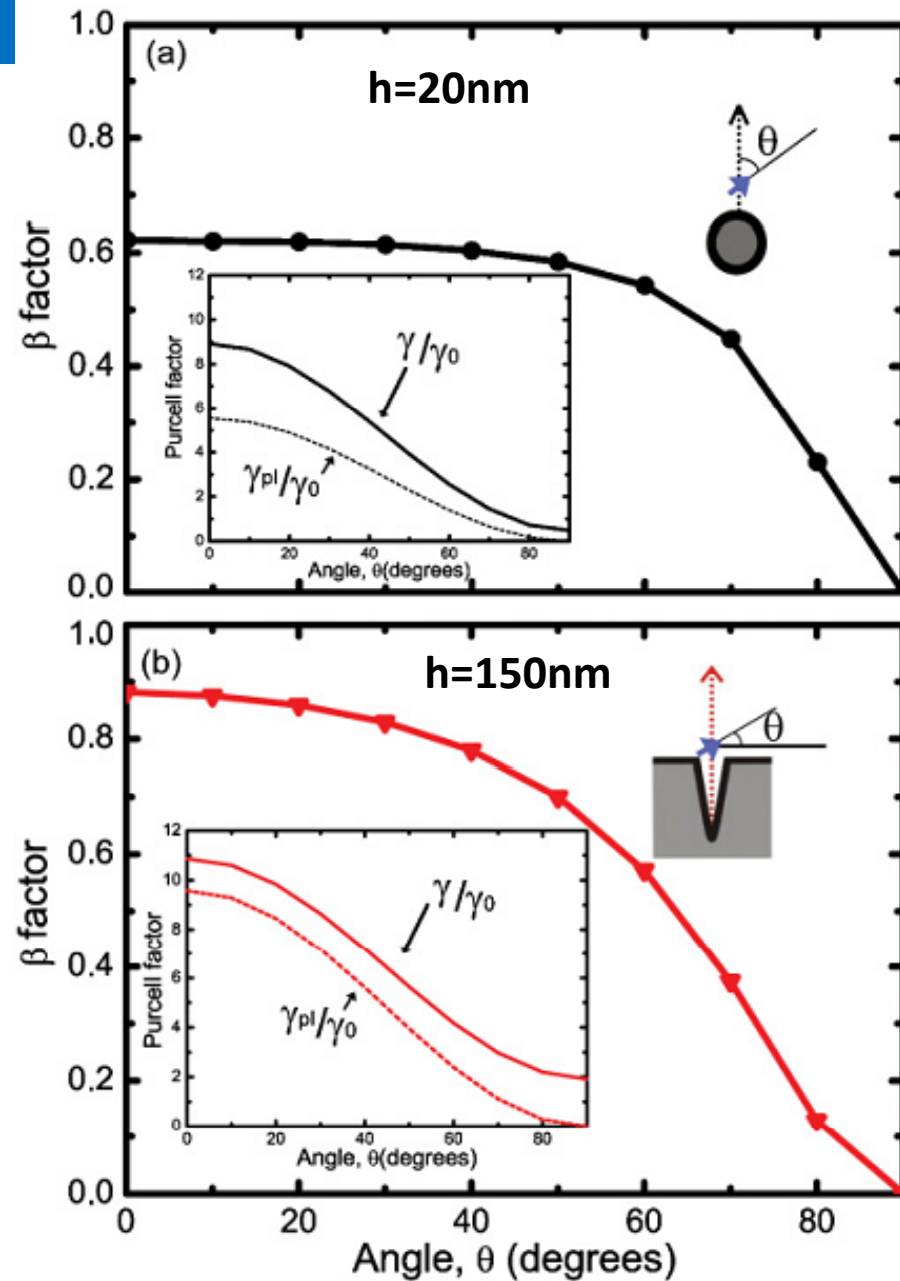
$$\text{Purcell factor} = \frac{\text{total radiation}}{\text{QE radiation to vacuum}} = \frac{\gamma}{\gamma_0}; \quad \beta \text{ factor} = \frac{\text{radiation to plasmons}}{\text{total radiation}} = \frac{\gamma_{pl}}{\gamma}$$



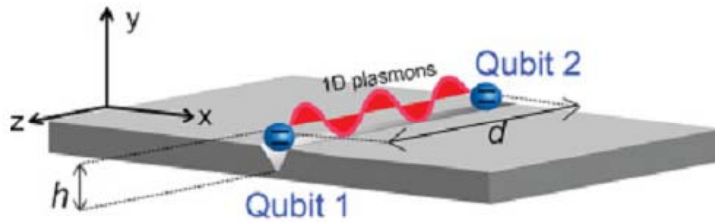
The channel is more convenient than the cylinder

β and Purcell factors

β - factor is very stable in a broad range of dipole orientations while Purcell factor decreases significantly when the dipole is not properly oriented

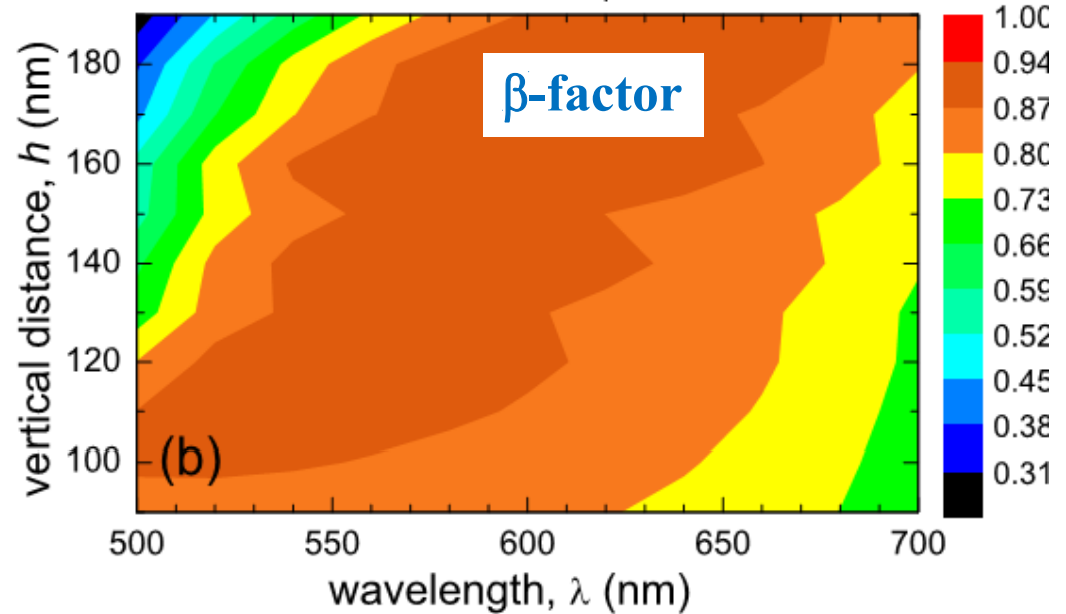
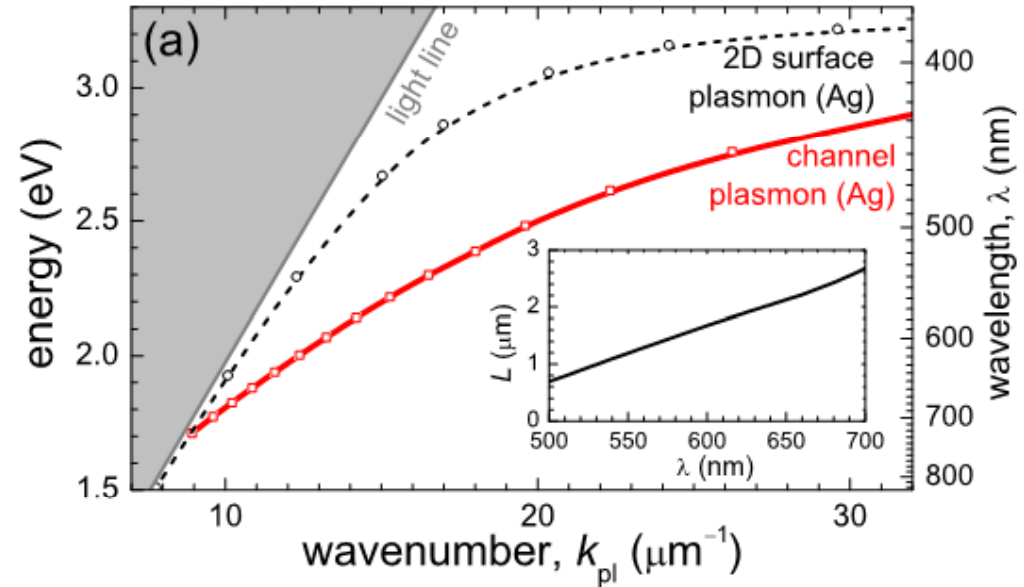


Dispersion & β factor for V-channel



$h=140\text{nm}$

V-angle= 20 degrees



Two QE's dynamics

All the degrees of freedom (SPP, dissipation, radiation) can be traced out producing effective coherent & incoherent interactions between the two QE's that can be computed from the classical Green's function:

$$\hat{H} = \int d^3\mathbf{r} \int_0^\infty d\omega \hbar \omega a^\dagger(\mathbf{r}, \omega) a(\mathbf{r}, \omega) + \sum_{i=1,2} \hbar \omega_0 \hat{\sigma}_i^\dagger \hat{\sigma}_i - \sum_{i=1,2} \int_0^\infty d\omega [\mathbf{d}_i \hat{\mathbf{E}}(\mathbf{r}_i, \omega) + h.c.]$$

$$\hat{\mathbf{E}}(\mathbf{r}, \omega) = i \sqrt{\frac{\hbar}{\pi \epsilon_0}} \frac{\omega^2}{c^2} \int d^3\mathbf{r}' \sqrt{\epsilon_i(\mathbf{r}', \omega)} \mathbf{G}(\mathbf{r}, \mathbf{r}', \omega) a(\mathbf{r}', \omega)$$

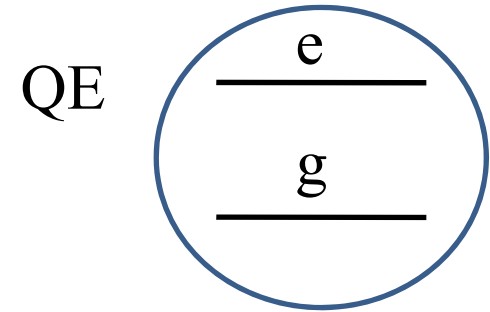
$$\frac{\partial \hat{\rho}}{\partial t} = -\frac{i}{\hbar} [\hat{H}_s + \hat{H}_L, \hat{\rho}] - \frac{1}{2} \sum_{i,j} \gamma_{ij} (\hat{\rho} \hat{\sigma}_i^\dagger \hat{\sigma}_j + \hat{\sigma}_i^\dagger \hat{\sigma}_j \hat{\rho} - 2 \hat{\sigma}_j \hat{\rho} \hat{\sigma}_i^\dagger)$$

$$\hat{H}_s = \sum_i \hbar(\omega_0 + \delta_i) \hat{\sigma}_i^\dagger \hat{\sigma}_i + \sum_{i \neq j} \hbar g_{ij} \hat{\sigma}_i^\dagger \hat{\sigma}_j \quad \hat{H}_L = -\frac{1}{2} \sum_i \hbar \Omega_i \hat{\sigma}_i^\dagger e^{i\omega_L t} + h.c.$$

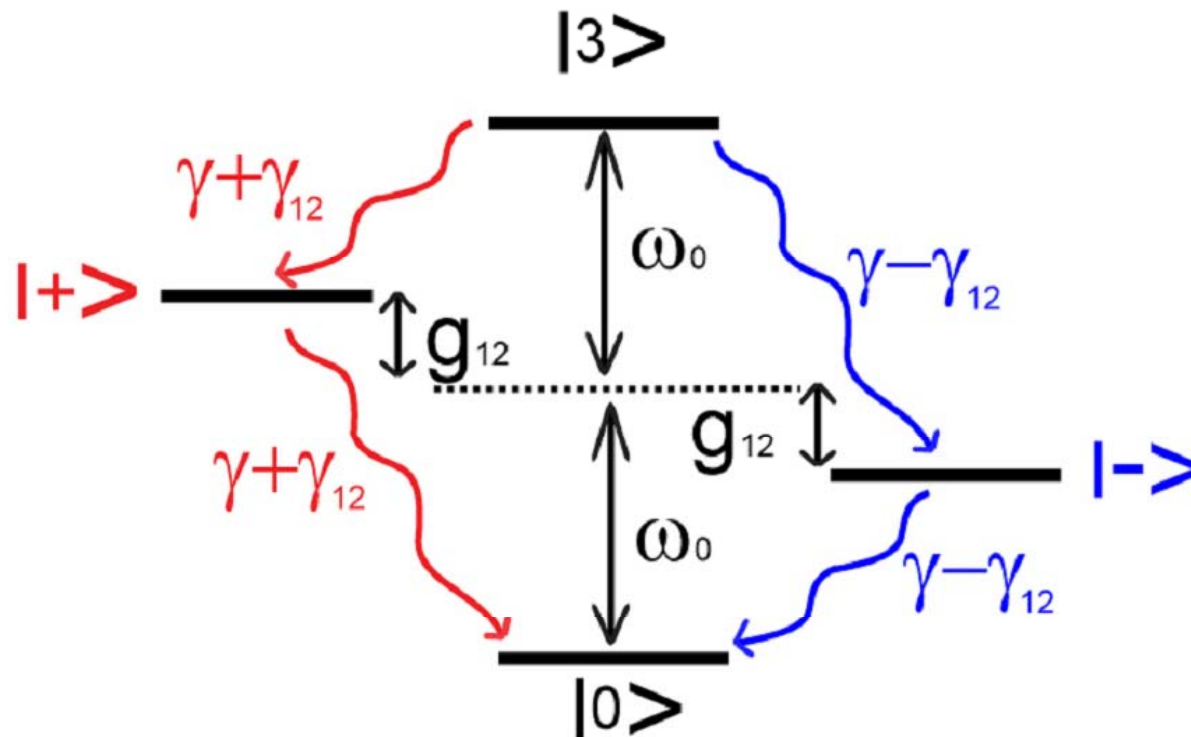
$$g_{ij} = \frac{\omega_0^2}{\hbar \epsilon_0 c^2} \mathbf{d}_i^* \text{Re} \mathbf{G}(\mathbf{r}_i, \mathbf{r}_j, \omega_0) \mathbf{d}_j$$

$$\gamma_{ij} = \frac{2\omega_0^2}{\hbar \epsilon_0 c^2} \mathbf{d}_i^* \text{Im} \mathbf{G}(\mathbf{r}_i, \mathbf{r}_j, \omega_0) \mathbf{d}_j$$

Scheme of levels



$$|3\rangle = |e_1 e_2\rangle \quad |0\rangle = |g_1 g_2\rangle \quad |\pm\rangle = \frac{1}{\sqrt{2}} (|g_1 e_2\rangle \pm |e_1 g_2\rangle)$$



Modulation of γ_{12} would allow to switch on/off **red** and **blue** paths

Two QE's dynamics

It is possible to identify the effects of SPP & dissipation

SPP Green's function



Effective interaction

$$\mathcal{L}(\rho) = J_{1,2}(\sigma_1 \rho \sigma_2^\dagger - \rho \sigma_2^\dagger \sigma_1) + h.c.$$

$$J_{1,2} = \frac{J(\omega_0)}{2} e^{iq(\omega_0)|x_1-x_2|}$$

$$\mathbf{G}_{SPP}(\mathbf{r}, \mathbf{r}') = \frac{i \mathbf{E}^t(\mathbf{r}^t) \otimes \mathbf{E}^t(\mathbf{r}'^t)}{2\omega\mu_0 \int_{S_\infty} dS \mathbf{u}_z (\mathbf{E}^t \times \mathbf{H}^{*t})} e^{ik(z-z')}$$

Coherent

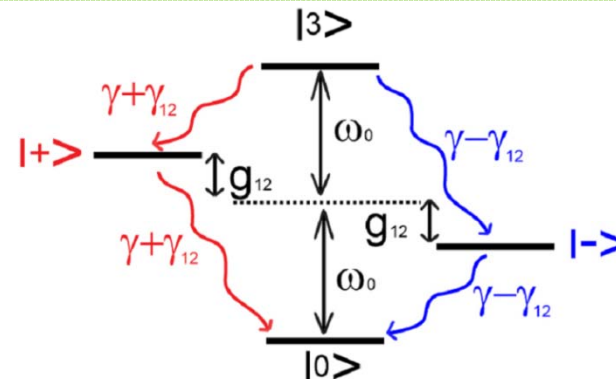
$$g_{ij} \simeq g_{ij,pl} = \frac{\gamma}{2} \beta e^{-d/2\ell} \sin(k_r d)$$

Incoherent

$$\gamma_{ij} \simeq \gamma_{ij,pl} = \gamma \beta e^{-d/2\ell} \cos(k_r d)$$

$\pi/2$ shift allows switching on/off

- Coherent versus incoherent interactions
- Control of different decay paths



Two QE's dynamics

It is possible to identify the effects of SPP & dissipation

SPP Green's function



Effective interaction

$$\mathcal{L}(\rho) = J_{1,2}(\sigma_1 \rho \sigma_2^\dagger - \rho \sigma_2^\dagger \sigma_1) + h.c.$$

$$J_{1,2} = \frac{J(\omega_0)}{2} e^{iq(\omega_0)|x_1 - x_2|}$$

$$\mathbf{G}_{SPP}(\mathbf{r}, \mathbf{r}') = \frac{i \mathbf{E}^t(\mathbf{r}^t) \otimes \mathbf{E}^t(\mathbf{r}'^t)}{2\omega\mu_0 \int_{S_\infty} dS \mathbf{u}_z (\mathbf{E}^t \times \mathbf{H}^{*t})} e^{ik(z-z')}$$

Coherent

$$g_{ij} \simeq g_{ij,pl} = \frac{\gamma}{2} \beta e^{-d/2\ell} \sin(k_r d)$$

Incoherent

$$\gamma_{ij} \simeq \gamma_{ij,pl} = \gamma \beta e^{-d/2\ell} \cos(k_r d)$$

$$\frac{\partial \hat{\rho}}{\partial t} = -\frac{i}{\hbar} [\hat{H}_s + \hat{H}_L, \hat{\rho}] - \frac{1}{2} \sum_{i,j} \gamma_{ij} (\hat{\rho} \hat{\sigma}_i^\dagger \hat{\sigma}_j + \hat{\sigma}_i^\dagger \hat{\sigma}_j \hat{\rho} - 2 \hat{\sigma}_j \hat{\rho} \hat{\sigma}_i^\dagger)$$

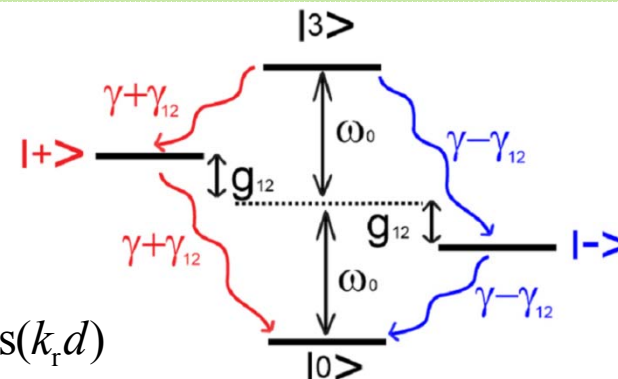
$$\hat{H}_s = \sum_i \hbar(\omega_0 + \delta_i) \hat{\sigma}_i^\dagger \hat{\sigma}_i + \sum_{i \neq j} \hbar g_{ij} \hat{\sigma}_i^\dagger \hat{\sigma}_j$$

$$\hat{H}_L = -\frac{1}{2} \sum_i \hbar \Omega_i \hat{\sigma}_i^\dagger e^{i\omega_L t} + h.c.$$

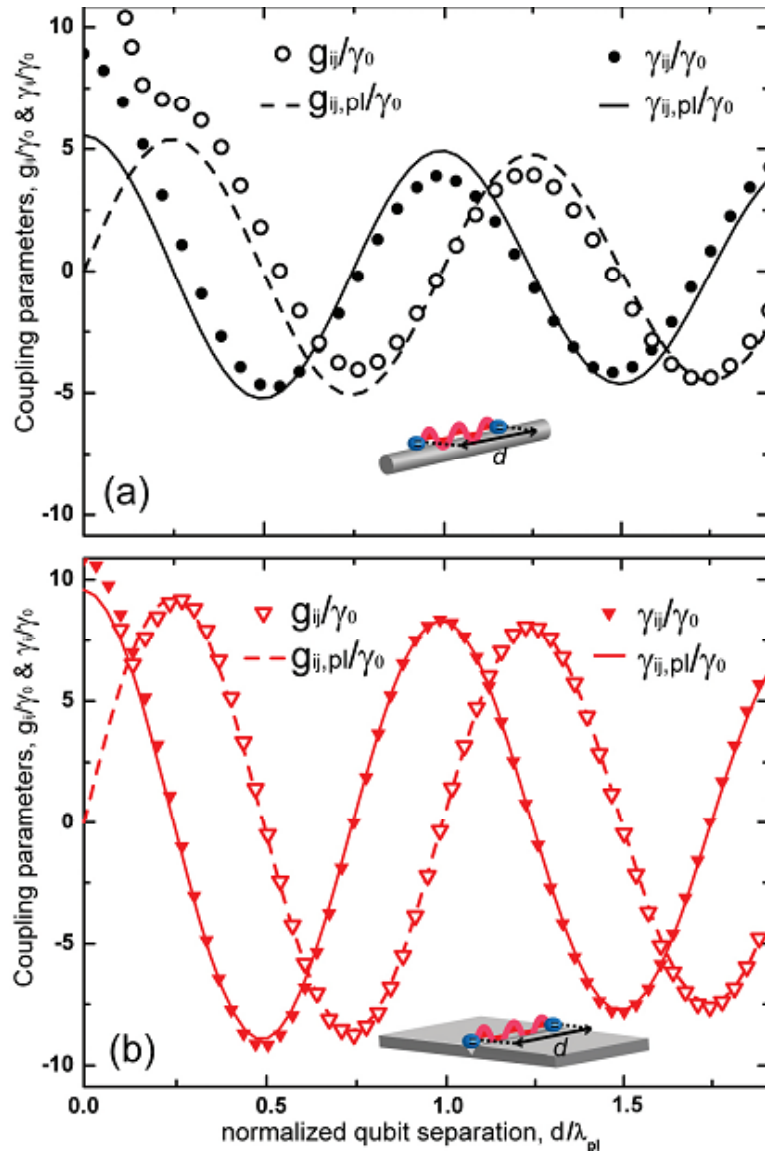
$\pi/2$ shift allows switching on/off

- Coherent versus incoherent interactions
- Control of different decay paths

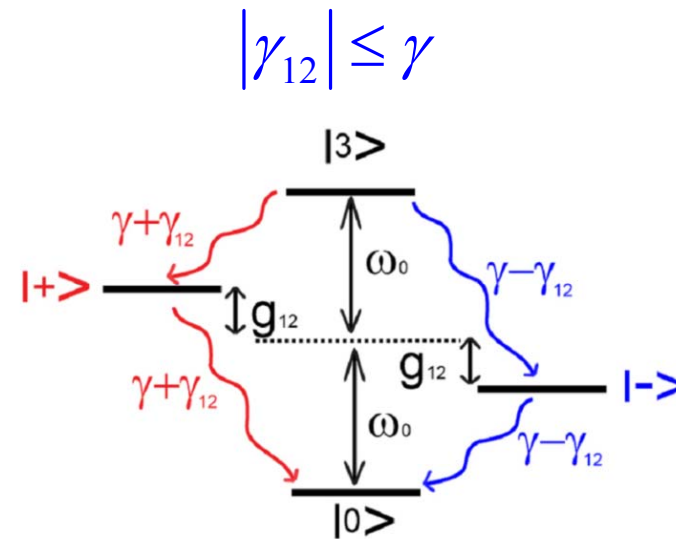
For inequivalent dipoles $\gamma_{ij,pl} = \sqrt{\gamma_{ii} \gamma_{jj}} \sqrt{\beta_i \beta_j} e^{-d/2\ell} \cos(k_r d)$



Coherent (g_{ij}) & incoherent (γ_{ij}) effective couplings between QE's



Incoherent coupling much more important than the coherent one because it switches on/off each decay path with respect to the other



Entanglement measure

Concurrence

Complex definition

Wooters, PRL 80, (1988)

$$\left\{ \begin{array}{l} C(\rho) = \max(0, \lambda_1 - \lambda_2 - \lambda_3 - \lambda_4) \\ R = \sqrt{\sqrt{\rho}\tilde{\rho}\sqrt{\rho}} \\ \tilde{\rho} = (\sigma_y \otimes \sigma_y)\rho^*(\sigma_y \otimes \sigma_y) \end{array} \right.$$

What we need to know: for **pure states**

Separable states (e.g. $|0\rangle$) $\Rightarrow C = 0$

Entangled states (e.g. $|-\rangle$) $\Rightarrow C = 1$

Entanglement measure

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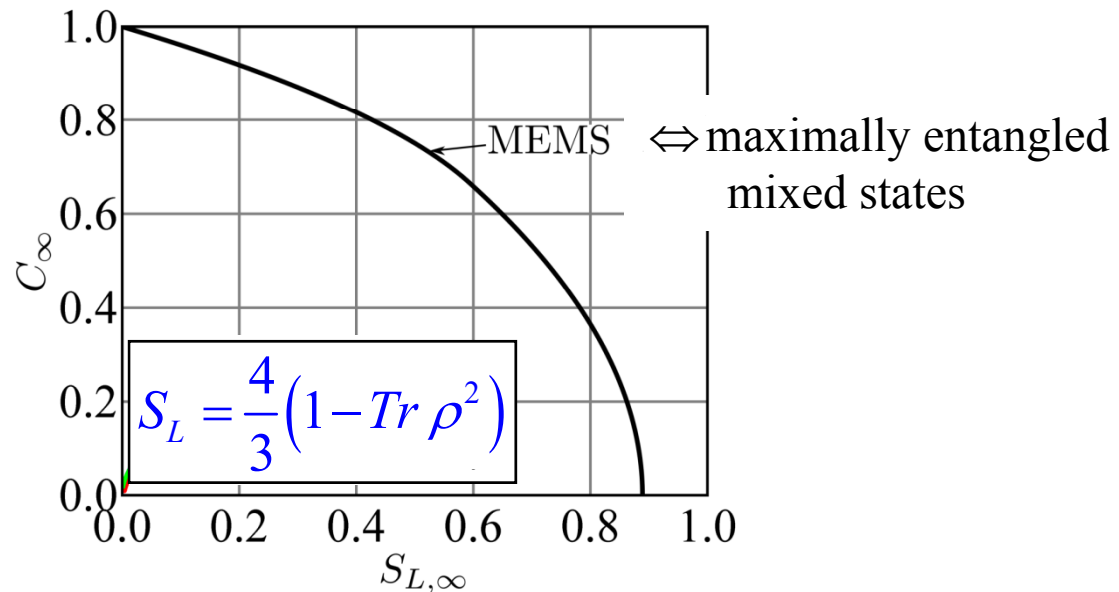
$$R = \sqrt{\sqrt{\rho} \tilde{\rho} \sqrt{\rho}}$$

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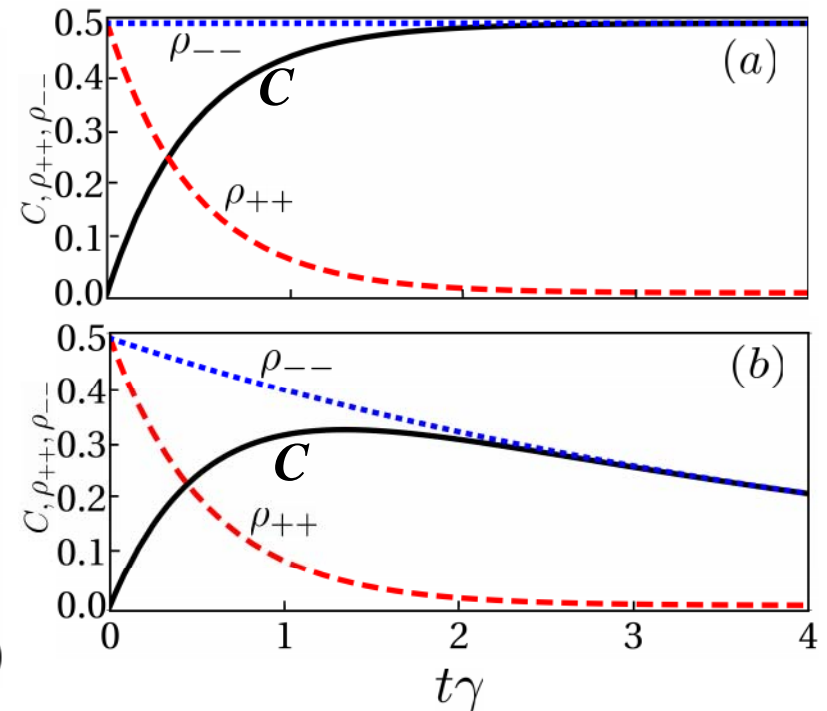
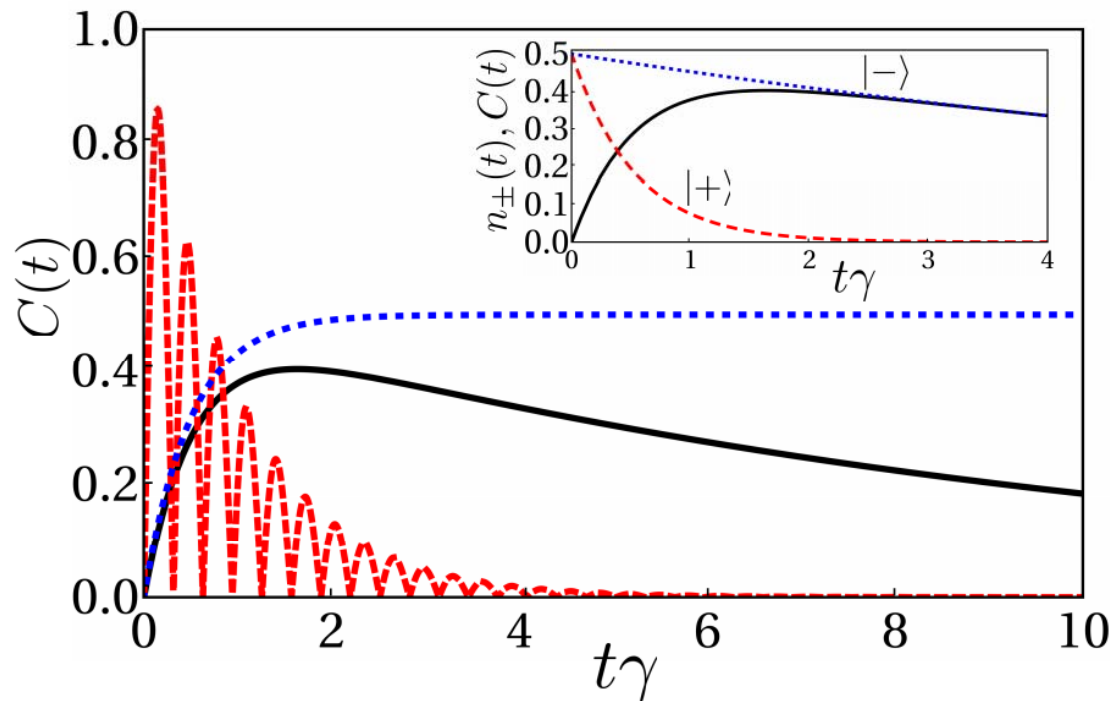
For mixed states:
Concurrence -
Linear entropy
diagram



Spontaneous decay of a single excitation

$|\psi(t=0)\rangle = |1\rangle = |e_1 g_2\rangle = \frac{1}{\sqrt{2}}(|+\rangle + |-\rangle) \Rightarrow$ **Concurrence becomes:**

$$C(t) = \sqrt{[\rho_{++}(t) - \rho_{--}(t)]^2 + 4\text{Im}[\rho_{+-}(t)]^2} = e^{-\gamma t} \sinh[\gamma\beta e^{-\lambda_{\text{pl}}/(2\ell)} t]$$



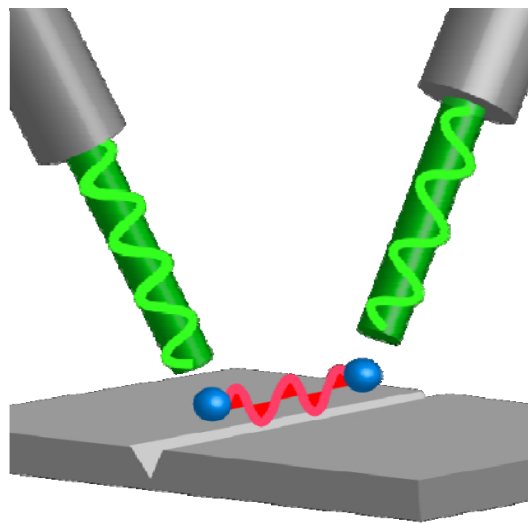
Stationary entanglement

(in the previous viewgraph) Spontaneous decay mediated by plasmons produces finite-time entanglement starting from an unentangled state

$$|\psi(t=0)\rangle = |1\rangle = |e_1 g_2\rangle = \frac{1}{\sqrt{2}}(|+\rangle + |-\rangle)$$

But one wants both to *obtain* and *manipulate* stationary entanglement.

This can be done by means of lasers:

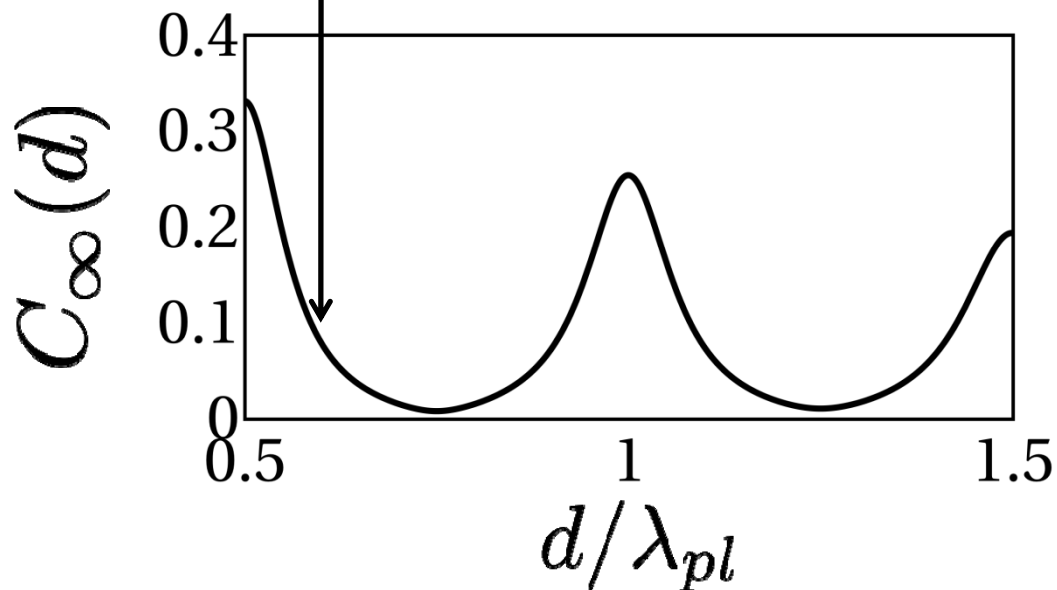
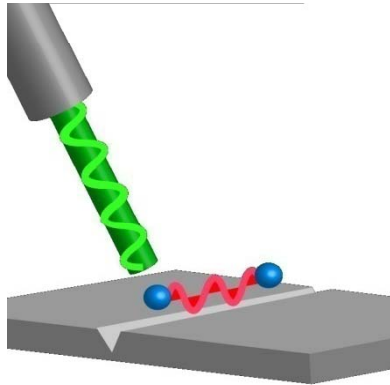


$$H_{las} = \sum_{i=1}^2 \Omega_i (\sigma_i + \sigma_i^\dagger)$$

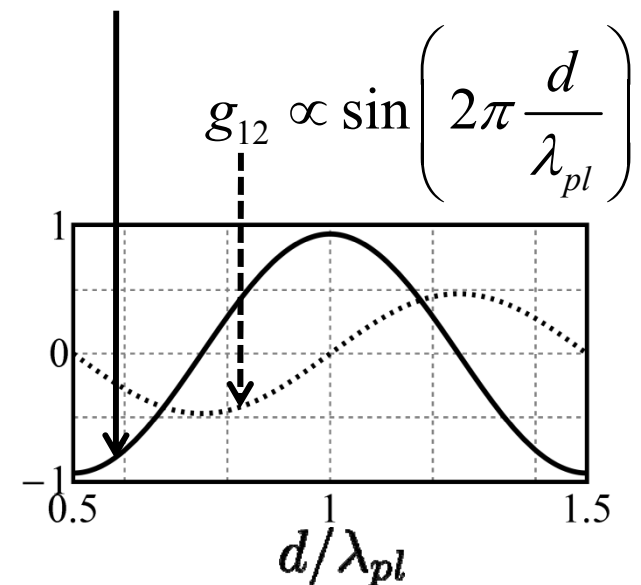
In the coherent part of the master equation

Stationary entanglement

$$\Omega_1 \neq 0, \Omega_2 = 0$$



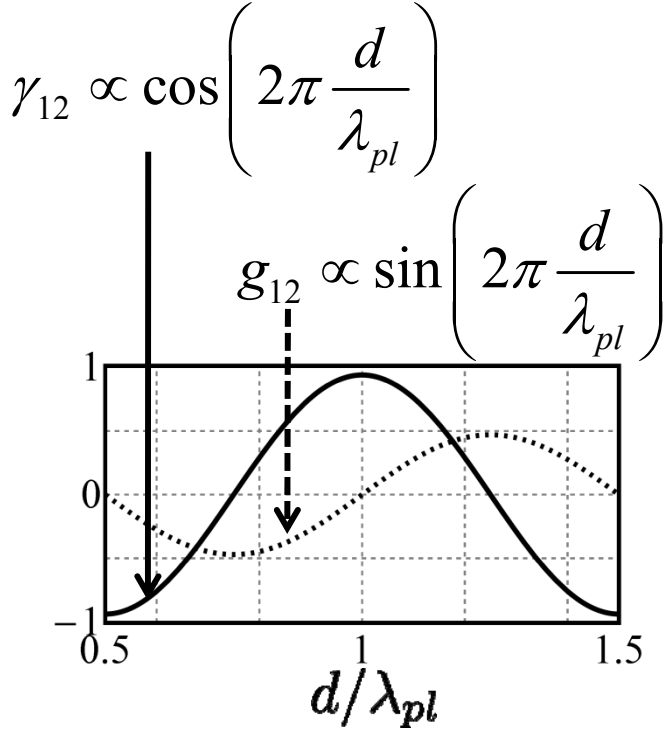
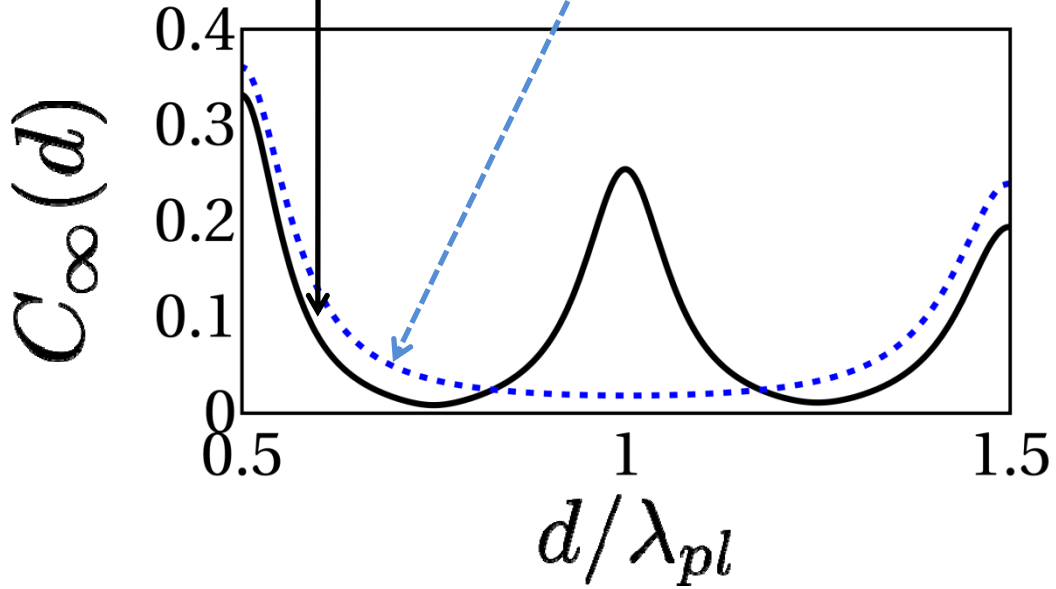
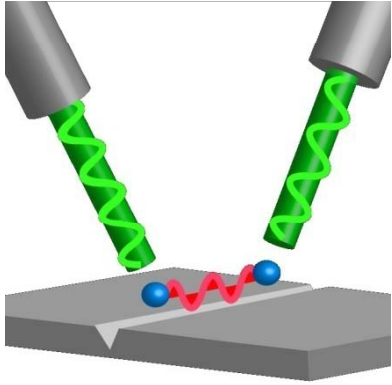
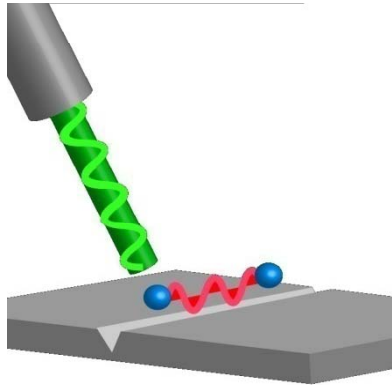
$$\gamma_{12} \propto \cos\left(2\pi \frac{d}{\lambda_{pl}}\right)$$



Stationary entanglement

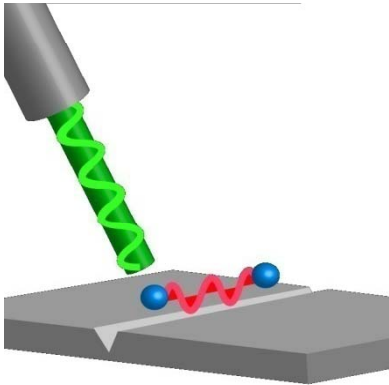
$\Omega_1 \neq 0, \Omega_2 = 0$

$\Omega_2 = \Omega_1$

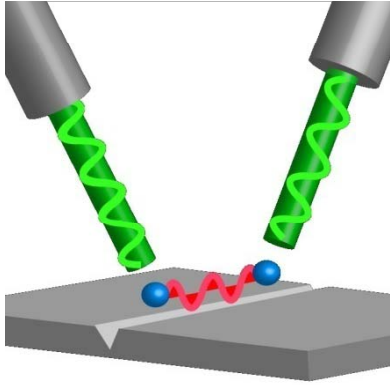


Stationary entanglement

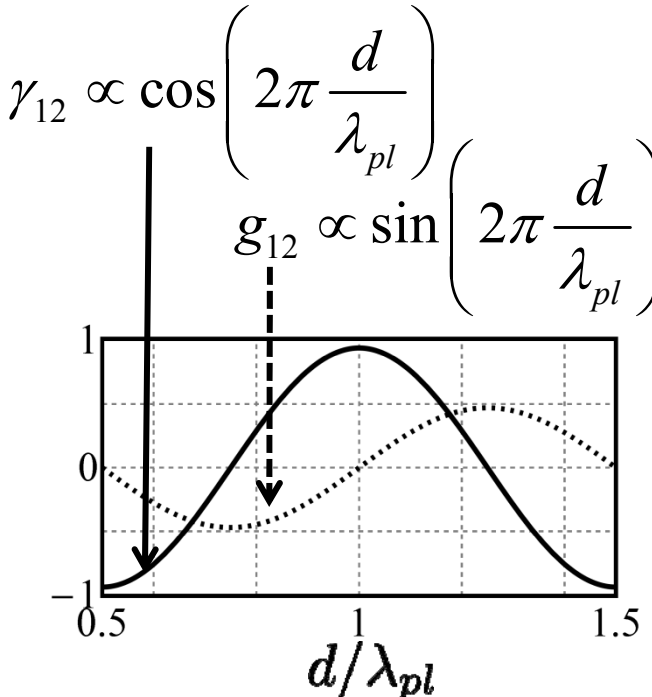
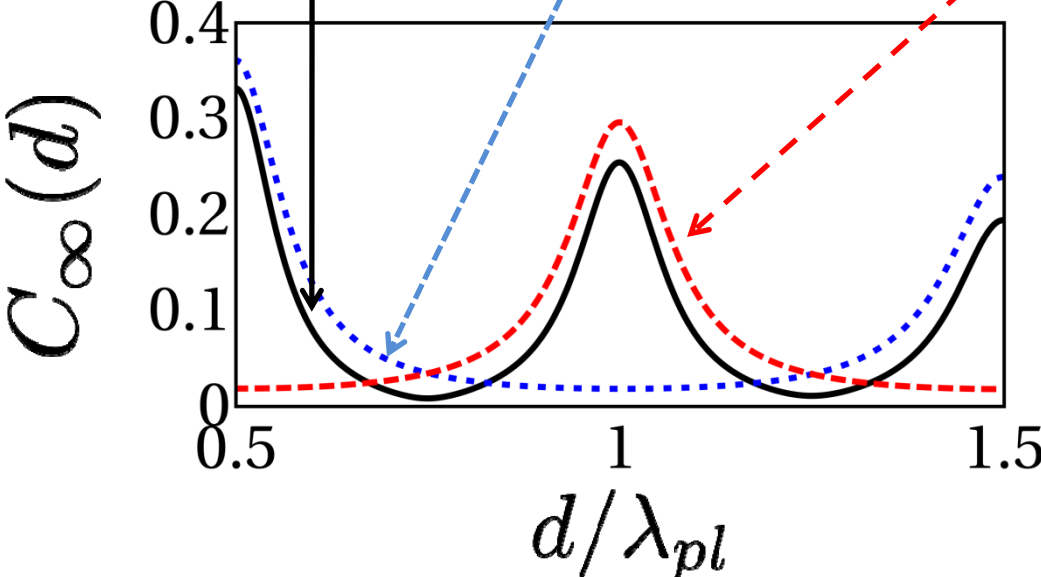
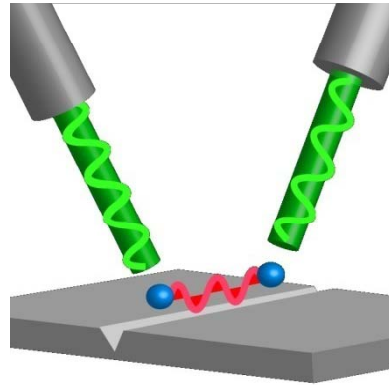
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$\Omega_1 = e^{i\pi} \Omega_2$



How is stationary entanglement generated?

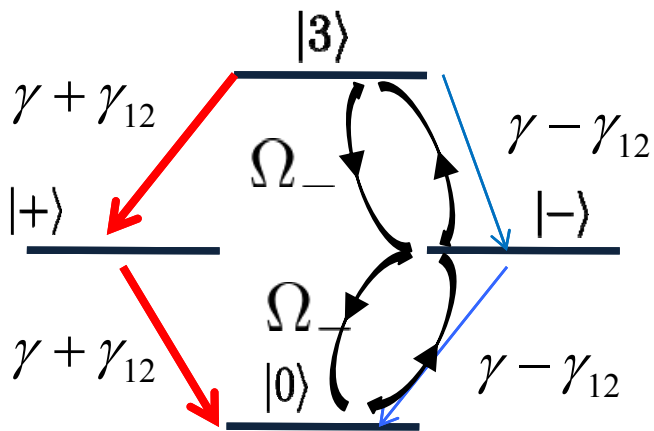
$$\gamma_{12} \propto \cos\left(2\pi \frac{d}{\lambda_{pl}}\right)$$

$$d \approx \lambda_{pl}$$

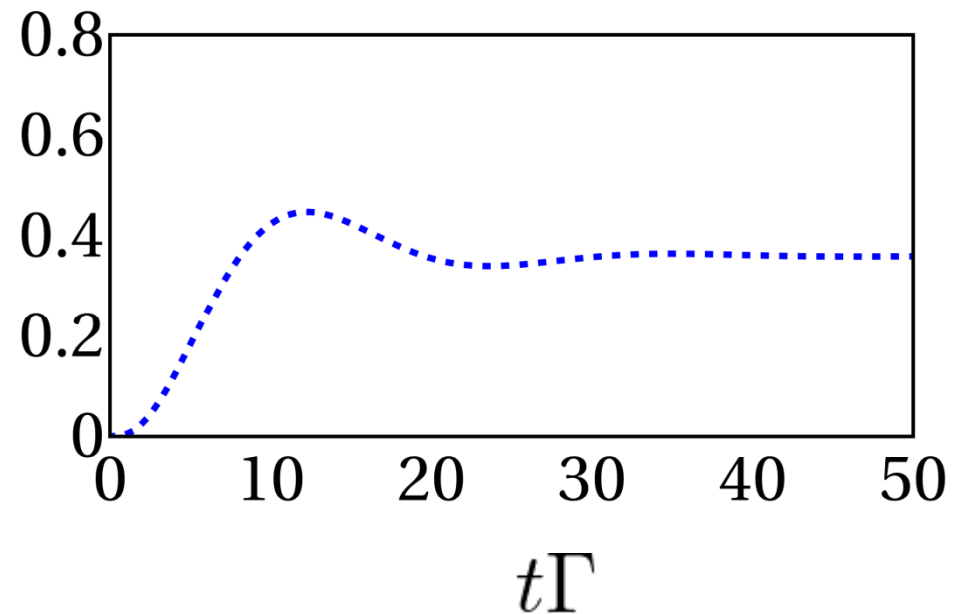
$$\Omega_1 = e^{i\pi} \Omega_2$$

$$\Omega_- = \frac{(\Omega_1 - \Omega_2)}{\sqrt{2}}$$

$$\left\{ \begin{array}{l} H_{las}|0\rangle = \Omega_-|-\rangle \\ H_{las}|-\rangle = \Omega_-(|0\rangle + |3\rangle) \\ H_{las}|+\rangle = 0 \\ H_{las}|3\rangle = \Omega_-|-\rangle \end{array} \right.$$



$C(t)$



How is stationary entanglement generated?

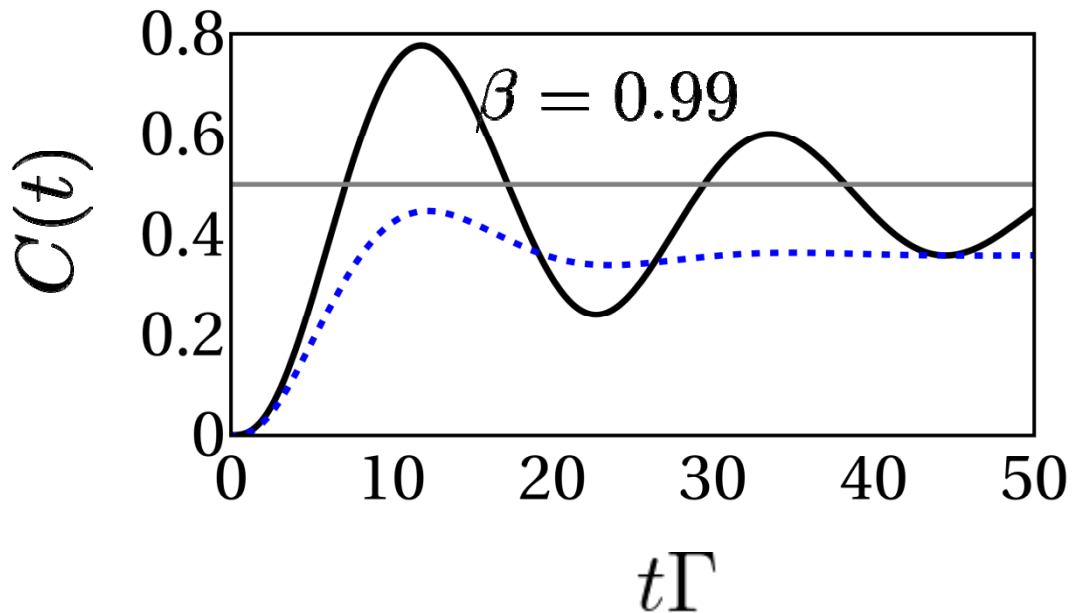
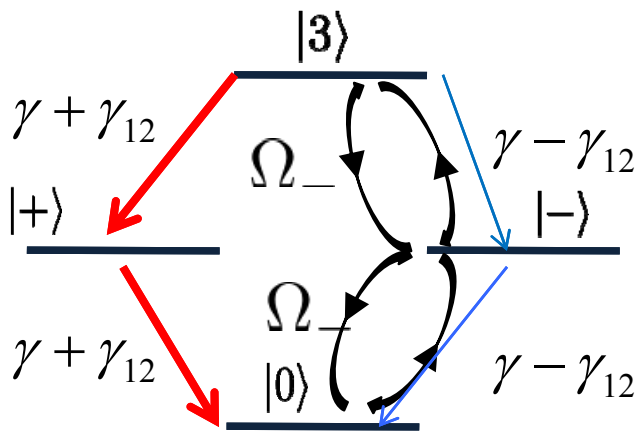
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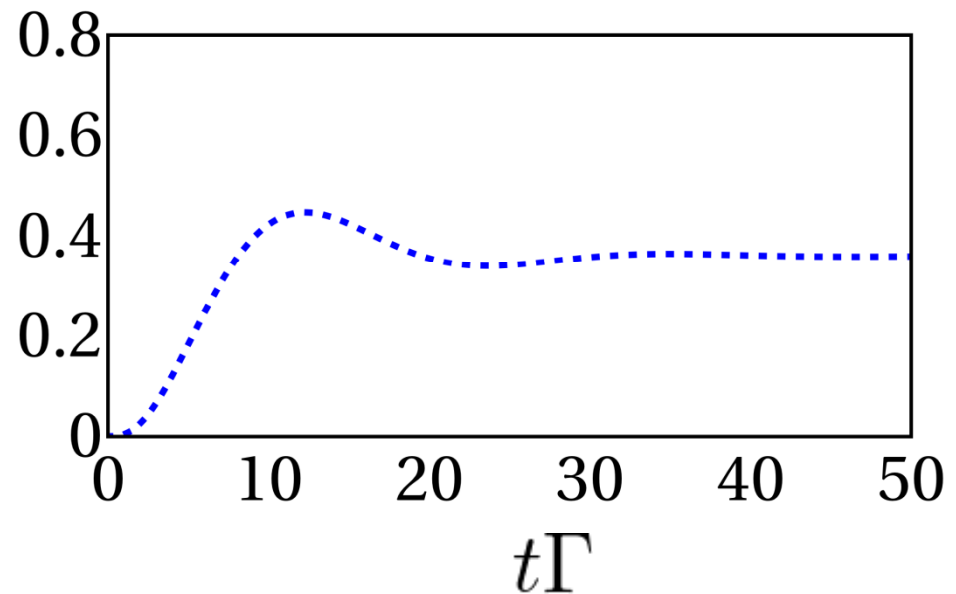
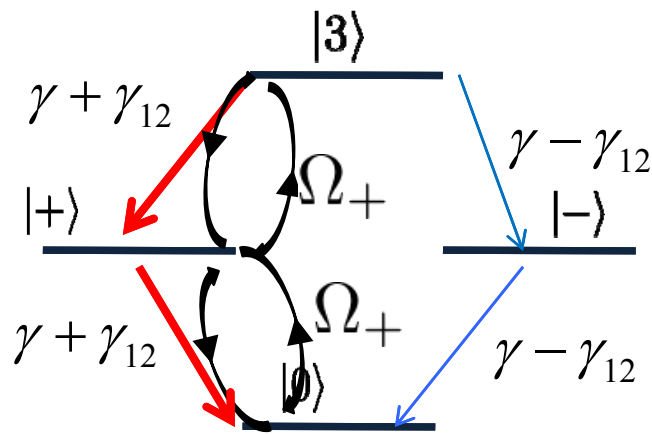
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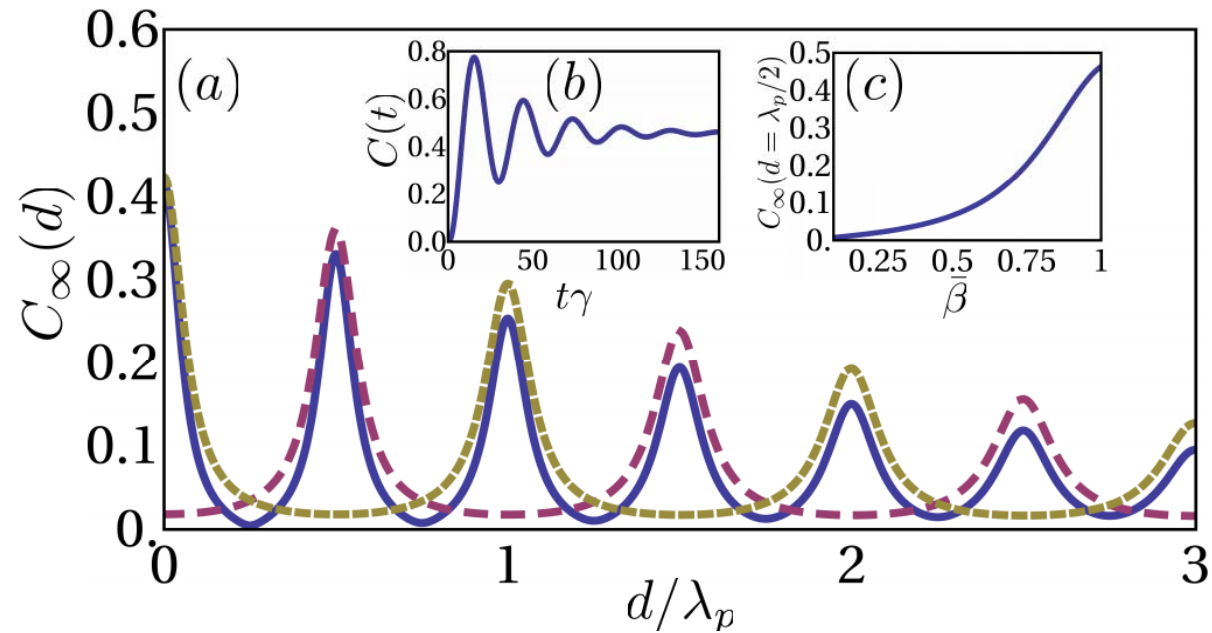
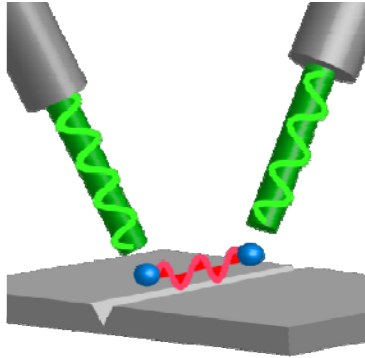
$$\Omega_1 = \Omega_2$$

$$\Omega_+ = \frac{(\Omega_1 + \Omega_2)}{\sqrt{2}}$$

$$\begin{cases} H_{las}|0\rangle = \Omega_+|+\rangle \\ H_{las}|-\rangle = 0 \\ H_{las}|+\rangle = \Omega_+(|0\rangle + |3\rangle) \\ H_{las}|3\rangle = \Omega_+|+\rangle \end{cases}$$



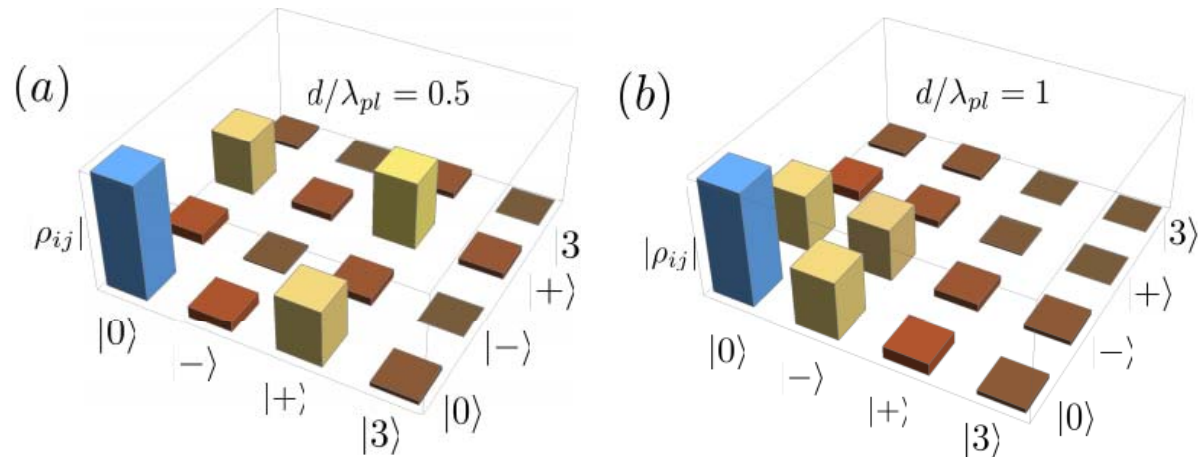
Stationary state concurrence



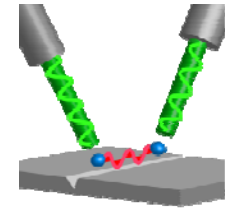
Stationary state tomography

Stationary
density matrix

$$\Omega_1 = 0.15\gamma, \quad \Omega_2 = 0$$



How to measure stationary concurrence: QE-QE correlation

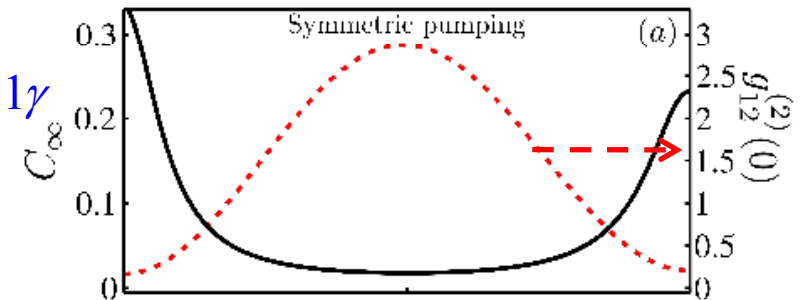


Second order cross-coherence

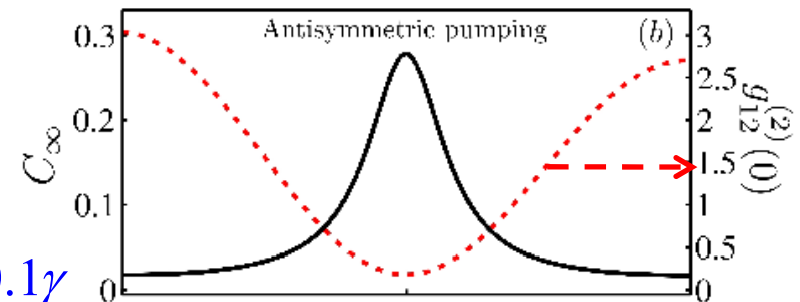
between the two QE's

$$g_{12}^{(2)} = \frac{\langle \sigma_1^\dagger \sigma_2^\dagger \sigma_2 \sigma_1 \rangle}{\langle \sigma_1^\dagger \sigma_1 \rangle \langle \sigma_2^\dagger \sigma_2 \rangle}$$

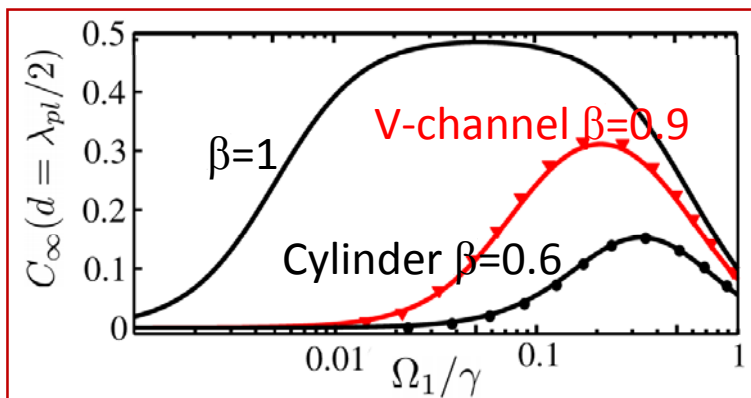
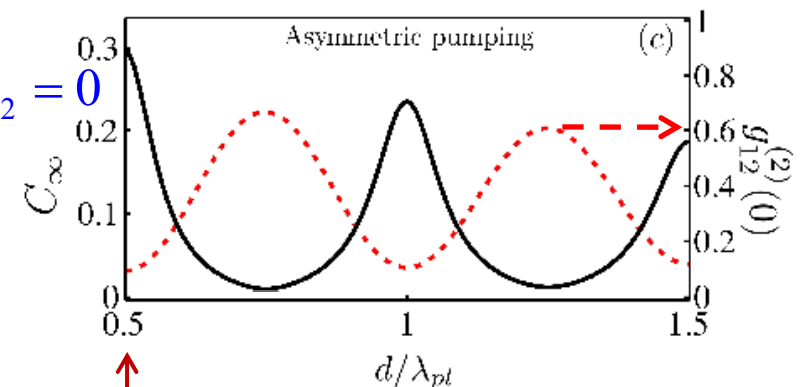
$$\Omega_1 = \Omega_2 = 0.1\gamma$$

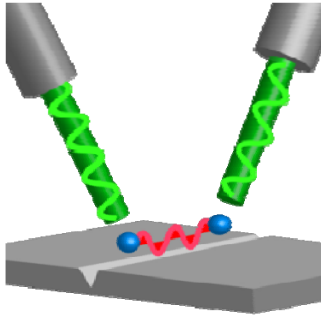


$$\Omega_1 = -\Omega_2 = 0.1\gamma$$



$$\Omega_1 = 0.15\gamma, \Omega_2 = 0$$

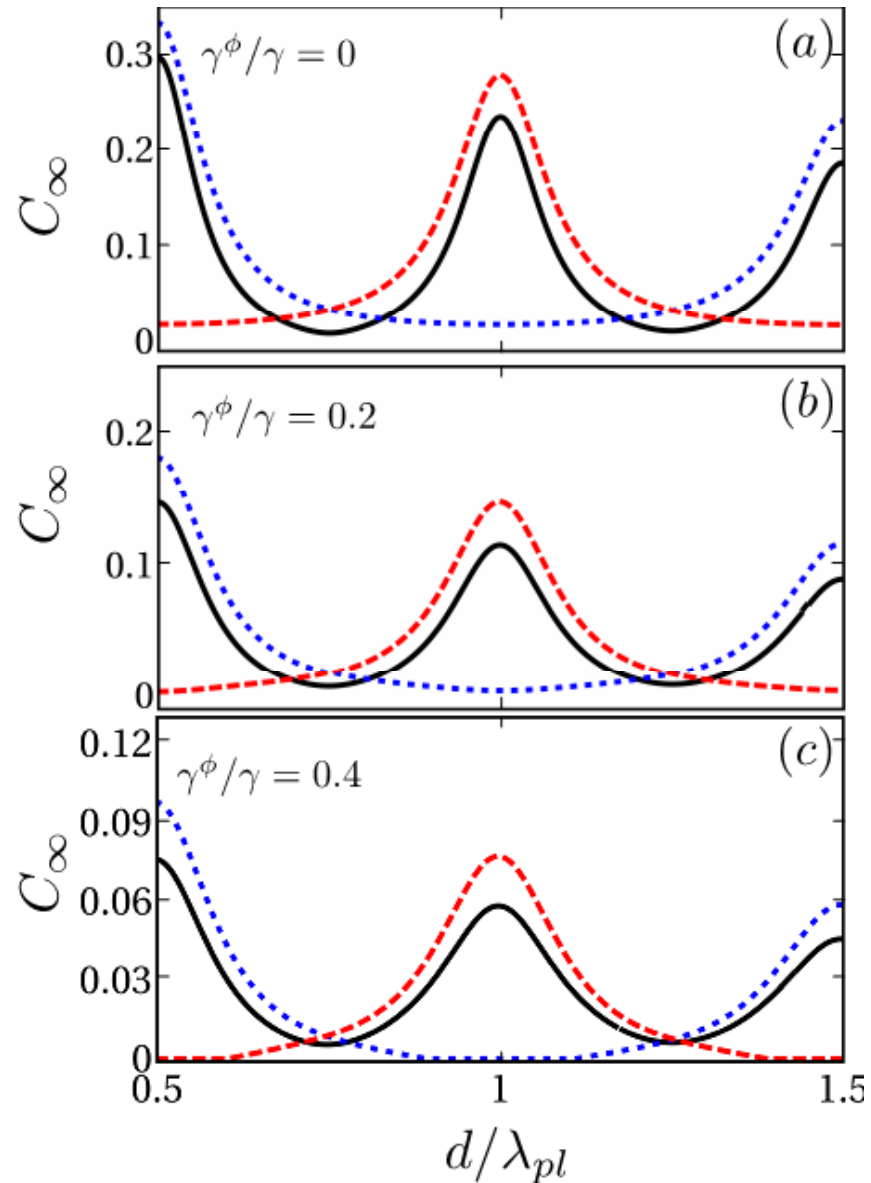




Effect of pure dephasing

$$\mathcal{L}_{\text{deph}}[\hat{\rho}] = \frac{\gamma^\phi}{2} \sum_i [[\hat{\sigma}_i^\dagger \hat{\sigma}_i, \hat{\rho}], \hat{\sigma}_i^\dagger \hat{\sigma}_i]$$

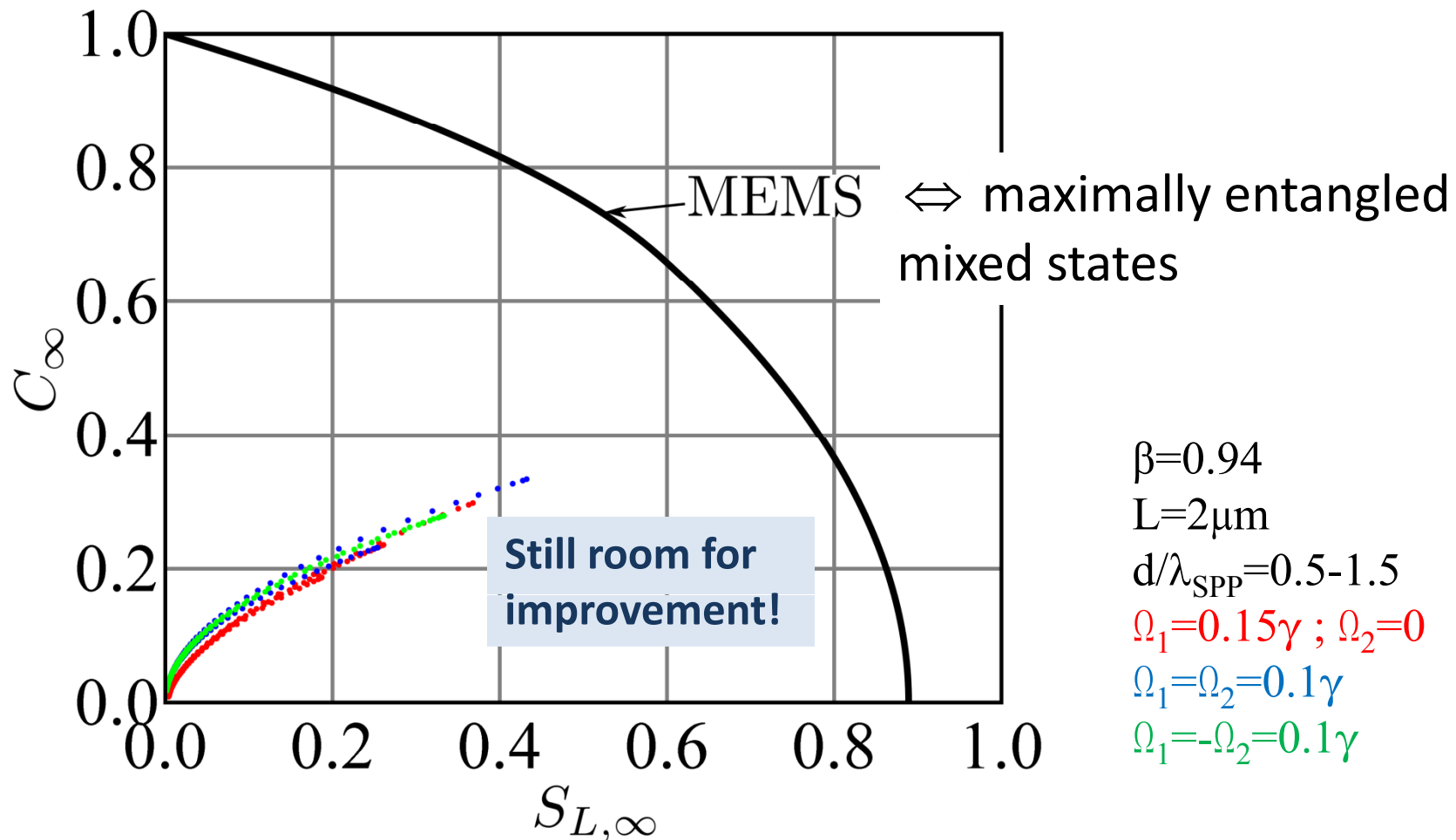
Pure dephasing reduces, but not critically, both correlations & concurrence



Purity

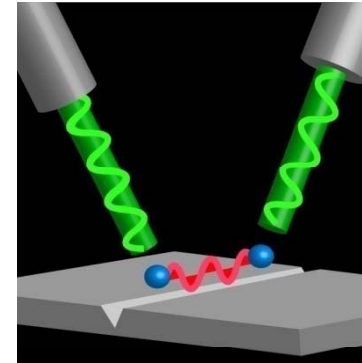
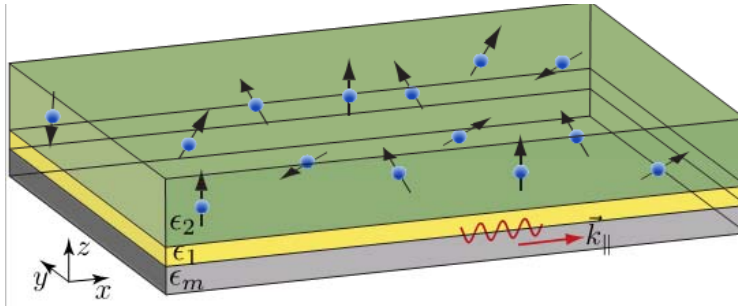
Concurrence - Linear entropy diagram

$$S_L = \frac{4}{3}(1 - \text{Tr } \rho^2)$$



Strong coupling to excitons &

SPP
Intermediary for quantum entanglement



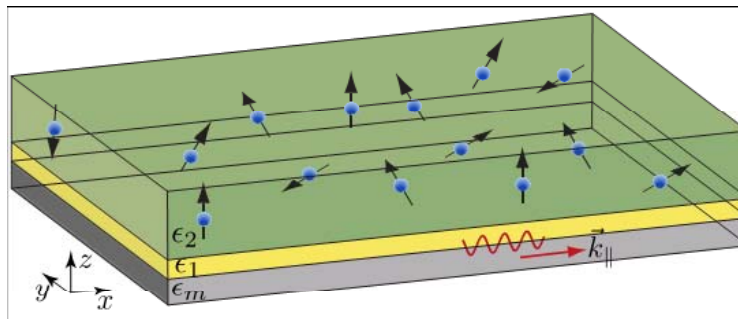
Outline

- Introduction to surface plasmon polaritons (SPP)
- Coupling of 1 quantum emitter (QE) to SPP
- Collective mode (excitons) strongly coupled to SPP
- Coupling & entanglement of 2 QE mediated by SPP
- **Conclusion**

Conclusion: Plasmon-polaritons share many properties & capabilities with cavity exciton-polaritons (Cav-QED).

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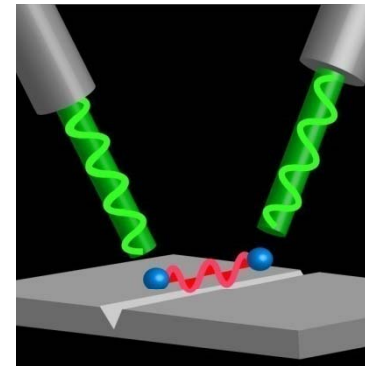
Strong coupling to excitons &



- A. Gonzalez-Tudela *et al*, Phys. Rev. Lett. **110**, 126891 (2013)

SPP

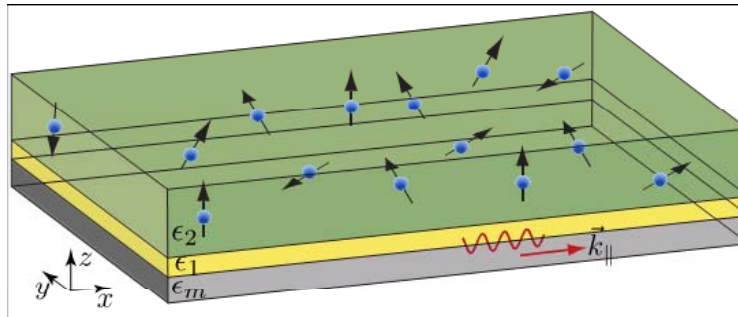
Intermediary for quantum entanglement



- A. Gonzalez-Tudela *et al*, Phys. Rev. Lett. **106**, 020501(2011)
- D. Martin-Cano, *et al*, Phys. Rev. B **84**, 235306 (2011)

Conclusion: Plasmon-polaritons share many properties & capabilities with cavity exciton-polaritons (Cav-QED).

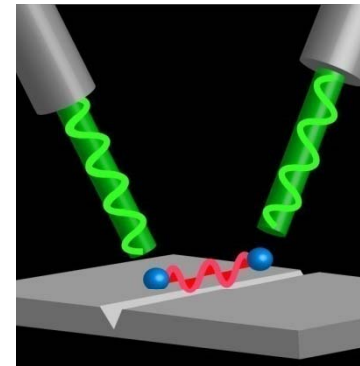
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Thanks for your attention